

# Persistent Monetary Non-neutrality in an Estimated Model with Menu Costs and Partially Costly

Information \*

Marco Bonomo  
Insper

Carlos Carvalho  
CBB and PUC-Rio

René Garcia  
EDHEC Business School

Vivian Malta  
World Bank

September 29, 2016

\*The views expressed in this paper are those of the authors and do not necessarily reflect the position of the Central Bank of Brazil.

# Motivation

---

- “Micro-macro disconnect”
  - Many large, frequent price changes
  - Aggregate evidence of large degree of monetary non-neutrality
- Models: Different pricing frictions → different micro and macro implications
  - menu costs → state-dependent rules that fit microdata reasonably well, but small non-neutrality (e.g. Almeida and Bonomo 2002, Golosov Lucas 2007)
  - information frictions → larger real effects of monetary shocks, but nominal price adjustments typically occur continuously (e.g. Reis 2006, Maćkowiak and Wiederholt 2009)
- Type of pricing friction and frequency of price adjustments → difficulties in matching micro and macro evidence

# What we do

---

- Propose new model of price-setting that reconciles:
  - micro evidence of nominal rigidity and relatively frequent price adjustments
  - macro evidence of persistent real effects of monetary shocks
- Methodology to solve the model
- Estimation by SMM using price-setting statistics derived from micro data for U.S. (courtesy of Oleksiy Kryvtsov)
- Effects of monetary shocks in estimated model

# What we do

---

- Model features
  - time- and state-dependent pricing:
    - costs of changing prices ( $K$ )
    - partial information freely available
    - remaining information entails lump-sum cost ( $F$ )

# What we do

---

- When idiosyncratic information is free and aggregate information is costly (corroborated by estimation), the model:
  - matches U.S. price-setting statistics
  - produces persistent macroeconomic effects
- Mechanism: free information about idiosyncratic shocks → frequent price adjustments and low frequency of aggregate information collection → persistent effects of aggregate shocks.
  - Reminiscent flavor of, e.g., Maćkowiak and Wiederholt (2009)
  - Estimated model matches price-setting statistics from micro data

## Some related work

---

- On optimal rules with information and adjustment costs:
  - Bonomo and Garcia (2002), Bonomo and Carvalho (2004, 2010), Gorodnichenko (2010), Abel, Eberly, and Panageas (2010), Alvarez, Guiso, and Lippi (2012), Alvarez, Lippi and Paciello (2011)
- On the mechanism: frequent updating wrt idiosyncratic shocks and infrequent updating wrt aggregate shocks:
  - Maćkowiak and Wiederholt (2009), Klenow and Willis (2007), Knotek (2009).

# Outline

---

**Partial information model**

**Costly information only**

**Estimation**

**Monetary non-neutrality**

# Partial information model

---

- $p_t^*$ : frictionless optimal price (full information; no menu cost)
- Adjustment cost  $K$ , information cost  $F$ 
  - a firm always has the option to pay  $K$  to adjust its price
  - a firm always has the option to pay  $F$  to have full information
- Firms' objective: minimize PDV of expected total costs
  - integral of flow profit losses:  $\propto (p_t - p_t^*)^2$
  - adjustment costs  $K$  and information costs  $F$



# Partial information model

---

- Firm forms probabilistic assessment of  $E_t(p_t - p_t^*)^2$

- We decompose:

$$\begin{aligned} E_t(p_t - p_t^*)^2 &= (p_t - E_t p_t^*)^2 + E_t(p_t^* - E_t p_t^*)^2 \\ &= (p_t - E_t p_t^*)^2 + \text{Var}_t(p_t^*), \end{aligned}$$

- $(p_t - E_t p_t^*)^2 =$  flow cost of deviating from the *expected* level of the frictionless optimal price
- $E_t(p_t^* - E_t p_t^*)^2 = \text{Var}_t(p_t^*) =$  expected flow cost from not continuously entertaining information about  $p_t^*$

# Partial information model

---

- $dp_{it}^* = \mu dt - \sigma_f dW_{ft} - \sigma_c dW_{ct}$ , where  $W_{ft}$  and  $W_{ct}$  are independent standard Wiener processes
- Information about  $W_{ft}$  is continuously and freely available, costless to process
- Full information about  $W_{ct}$  entails lump-sum cost  $F$
- Define *time elapsed since the last information date*:

$$\tau = t - t_0$$

- And *expected price discrepancy*:

$$z_t = p_t - E_t p_t^*$$

# Partial information model

---

- Thus:

$$\begin{aligned} E_t(p_t - p_t^*)^2 &= z_t^2 + \text{Var}_t(p_t^*) \\ &= z_t^2 + \sigma_c^2 \tau \end{aligned}$$

- In the inaction (no adjustment or info. collection) range  $z_t$  and  $\tau$  will evolve as:

$$dz_t = -\mu dt + \sigma_f dW_{ft}$$

and

$$d\tau = dt$$

# Partial information model

---

- $V(z_t, \tau)$ : optimized value of the firm's dynamic cost-minimization problem
- Bellman equation in the (adjustment/information) inaction region:

$$V(z_t, \tau) = \left( z_t^2 + \sigma_c^2 \tau \right) dt + e^{-\rho dt} E_t V(z_{t+dt}, \tau + dt) \quad (1)$$

- The differential form of the Bellman equation (1) is written as (Ito's lemma):

$$\frac{1}{2} \sigma_f^2 V_{zz}(z, \tau) - V_z(z, \tau) \mu + V_\tau(z, \tau) - \rho V(z, \tau) + z^2 + \sigma_c^2 \tau = 0.$$

# Partial information model - the adjustment decision

---

- Adjustment inaction region  $\{l(\tau), c(\tau), u(\tau)\}$

- Lump-sum adjustment costs:

$$c(\tau) = \arg \min_z V(z, \tau)$$

- Adjustment always an option:

$$V(z, \tau) \leq V(c(\tau), \tau) + K$$

- Boundaries of inaction region satisfy:

$$\begin{aligned} V(l(\tau), \tau) &= V(c(\tau), \tau) + K \\ V(u(\tau), \tau) &= V(c(\tau), \tau) + K \end{aligned}$$

# Partial information model - the information decision

---

- Information policy  $\tau^*(z)$
- When information is collected at time  $\tau$ , history of  $W_{ct}$  is revealed:
  - Expected discrepancy  $z_t$  receives a shock with distribution  $N(0, \sigma_c^2 \tau)$
  - Time elapsed  $\tau$  is reset to zero
  - $V(z, \tau)$  becomes  $V(z + \sigma_c \sqrt{\tau} \varepsilon, 0)$ , which is uncertain before information collection.

# Partial information model - the information decision

---

- Since paying  $F$  and collecting/processing information is always an option, it must be true that

$$\forall (z, \tau), \quad V(z, \tau) \leq E \left[ V \left( z + \sigma_c \sqrt{\tau} \varepsilon, 0 \right) \right] + F$$

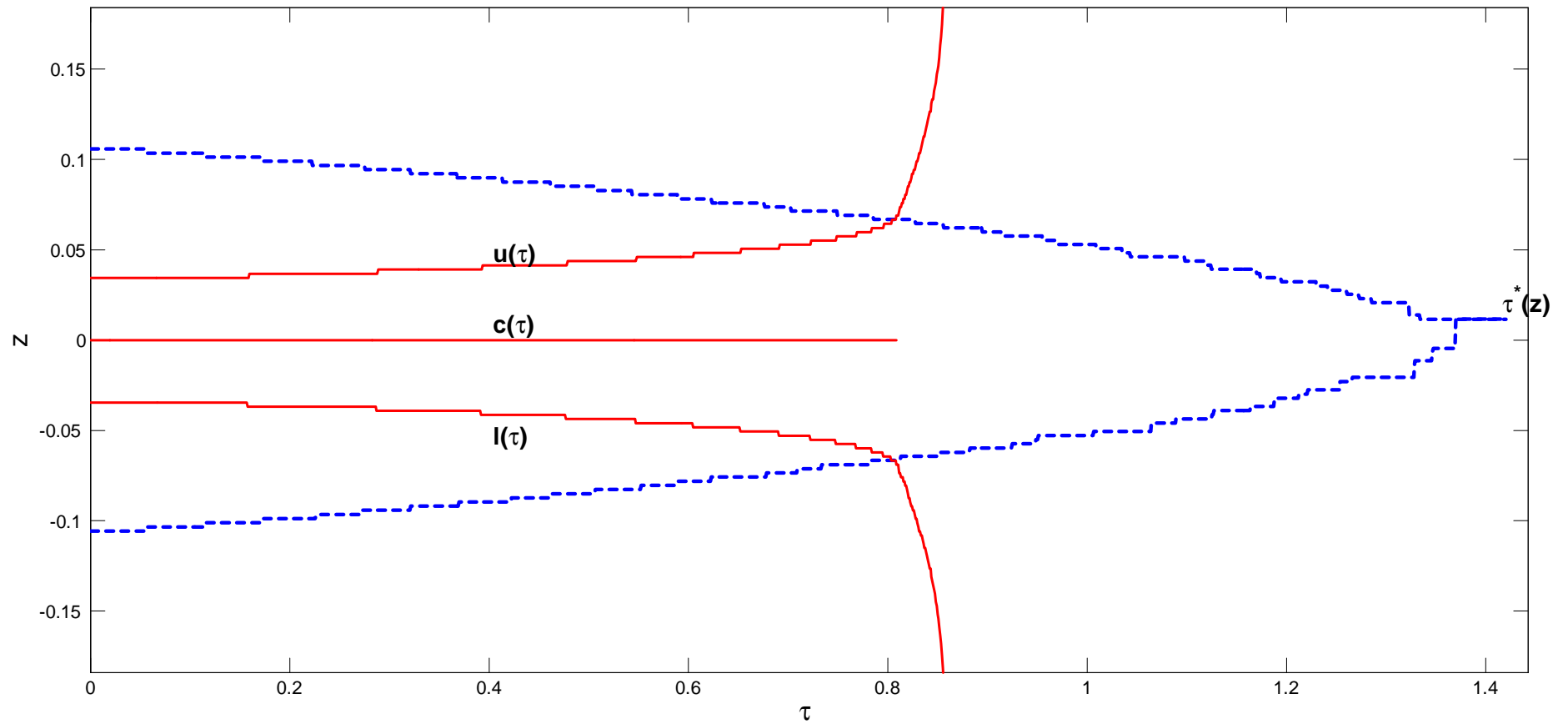
- The boundaries of the information inaction region satisfy:

$$V(z, \tau^*(z)) = E \left[ V \left( z + \sigma_c \sqrt{\tau^*(z)} \varepsilon, 0 \right) \right] + F$$

# Partial information model

Optimal Pricing Policy under Menu Costs and Partially Costly Information:

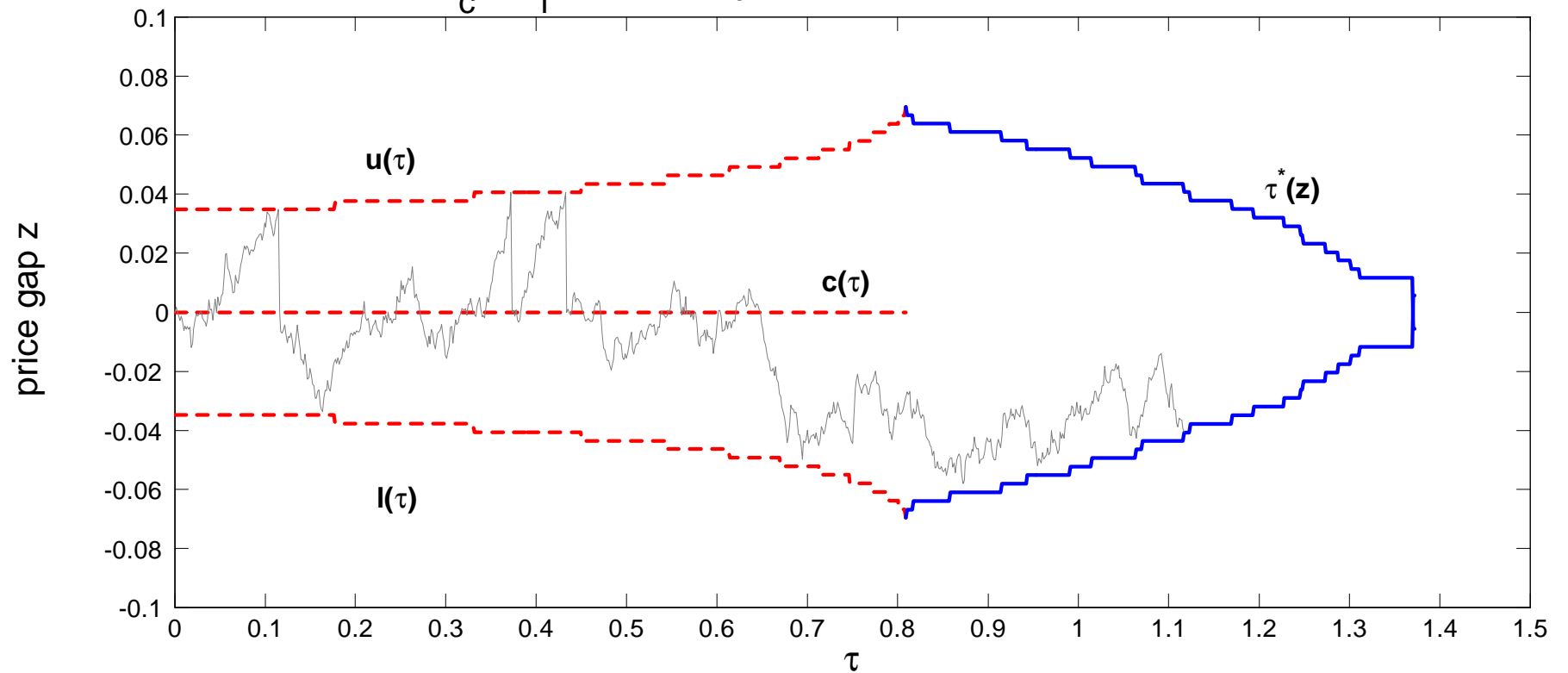
$$\mu=0, \sigma_c=0.1/\sqrt{2}, \sigma_f=0.1/\sqrt{2}, \rho=0.025, K=0.0005, F=0.0025$$





# Partial information model

$$\mu = 0, \sigma_c = \sigma_f = 0.1/\sqrt{2}, \rho = 0.025, K = 0.0005, F = 0.0025$$



# Costly information only

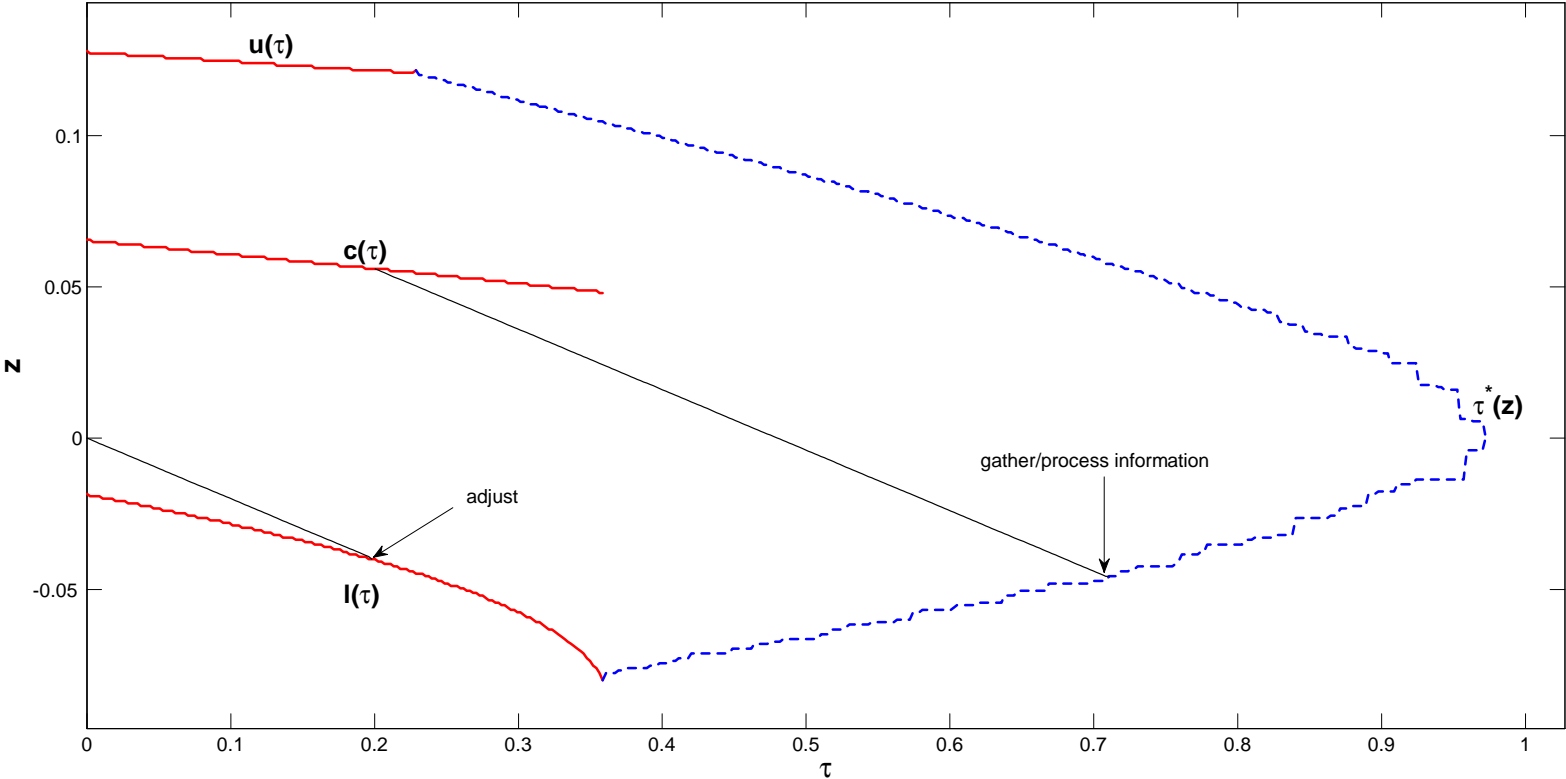
---

- Case studied by Alvarez, Lippi and Paciello (2011)
- Adjustments only on information (“observation”) dates
- We allow adjustments without information
  - likely to occur when inflation is high or  $K \ll F$
- Particular case of our model with  $W_{ft} \equiv 0$ , “ $\sigma_c = \sqrt{\sigma_c^2 + \sigma_f^2}$ ”

# Costly information only

Optimal Pricing Policy under Menu Costs with Costly Information Only:

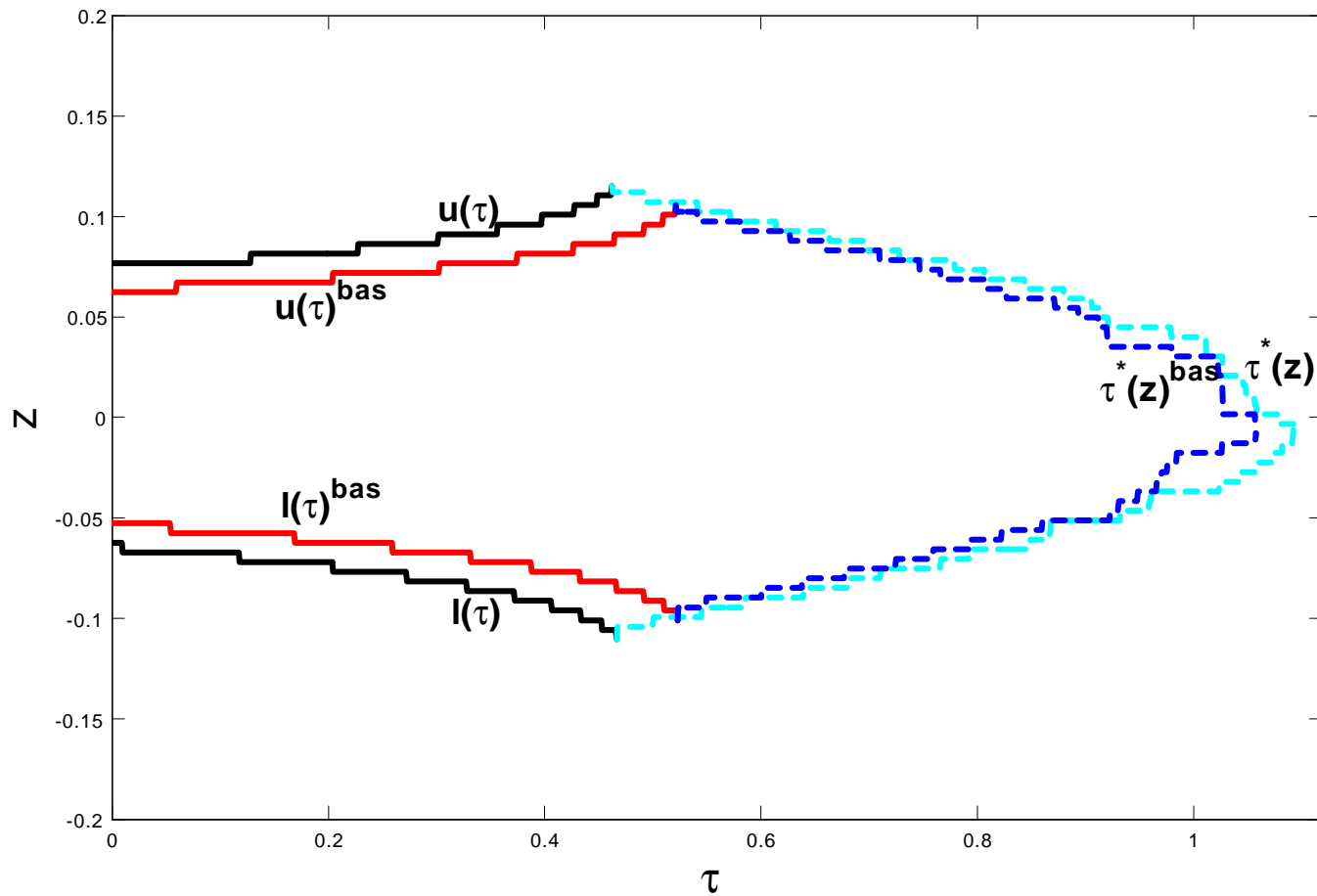
$\mu=0.2, \sigma=0.1, \rho=0.025, K=0.002, F=0.002$



# Price setting exercises Increase K

Optimal Pricing Policy under Menu Costs and Partially Costly Information ( $\sigma_a = \sigma_c$ ):

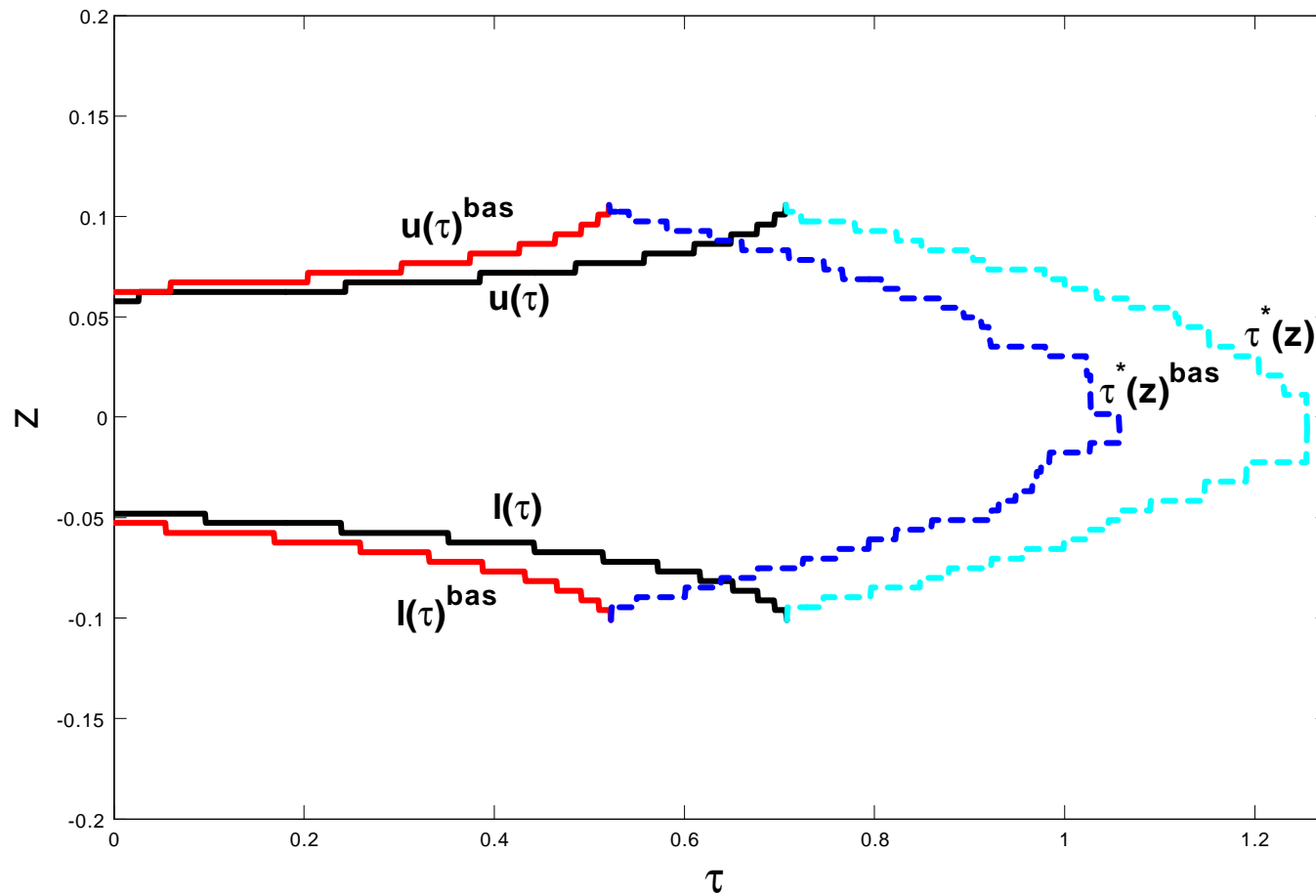
$\mu=0.0329$ ,  $\sigma_c=0.0999$ ,  $\sigma_f=0.1459$ ,  $\rho=0.025$ ,  $K=0.00114$  ( $\times 150\%$ ),  $F=0.00211$



# Price setting exercises Increase F

Optimal Pricing Policy under Menu Costs and Partially Costly Information ( $\sigma_a = \sigma_c$ ):

$\mu=0.0329, \sigma_c=0.0999, \sigma_f=0.1459, \rho=0.025, K=0.00076, F=0.003165 (\times 150\%)$



# Taking models to the data

---

- $W_{ft}, W_{ct}$  become  $W_{at}, W_{it}$
- 3 different models
  - idiosyncratic information free, aggregate information costly
  - aggregate information free, idiosyncratic information costly
  - both aggregate and idiosyncratic information costly

# Estimation

---

- Data: monthly price-setting statistics (regular prices) from Klenow-Kryvtsov
- Simulation Methods of Moments (calibrating  $\mu, \rho$ ), estimate  $\sigma_a, \sigma_i, F, K$  to target  $fr(\Delta p > 0), fr(\Delta p < 0), mean |\Delta p|, median |\Delta p|, (fr(\Delta p > 0))^2$
- Choice of moments:
  - higher  $\sigma_a \rightarrow$  more variable frequency of adjustments
  - given  $\mu > 0$ , higher  $\sigma_i \rightarrow$  reduces  $(freq \Delta p > 0) - (freq \Delta p < 0)$
  - lower  $F \rightarrow$  increases the proportion of informed adjustments – larger and more variable  $\rightarrow$  changes the relation between the mean and the median of  $|\Delta p|$ 
    - in the case of costly aggregate info.  $\rightarrow$  more variable frequency of adjustments.
  - higher  $K \rightarrow$  reduces both  $(freq \Delta p > 0)$  and  $(freq \Delta p < 0)$

# Estimation

---

$$\min_{\Phi} \left\{ (\Psi_{data} - \Psi_{sim}(\Phi))^T W^* (\Psi_{data} - \Psi_{sim}(\Phi)) \right\}$$

where

$$\Phi = \{\sigma_a, \sigma_i, F, K\}.$$

and

$$\Psi = \left\{ \begin{array}{l} [(fr \Delta p > 0)_t, (fr \Delta p < 0)_t]_{t=1}^T, \\ [(mean |\Delta p|)_t, (median |\Delta p|)_t]_{t=1}^T, \\ [(fr \Delta p > 0)_t^2]_{t=1}^T \end{array} \right\}$$



# Estimation results

---

Estimated Parameters				
	$\sigma_a$	$\sigma_i$	$F$	$K$
<b>No Partial Info</b>	<b>0.0254</b>	<b>0.1905</b>	<b>0.00065</b>	<b>0.00024</b>
standard deviation	0.0013	0.0025	1.36e-05	1.03e-05
t-statistic	19.9	74.8	48.0	23.1
<b>Partial Info (<math>\sigma_a = \sigma_c</math>)</b>	<b>0.0999</b>	<b>0.1459</b>	<b>0.00211</b>	<b>0.00076</b>
standard deviation	0.0004	0.0066	0.0002	0.0002
t-statistic	216.3	22.0	11.6	4.5
<b>Partial Info (<math>\sigma_a = \sigma_f</math>)</b>	<b>0.0181</b>	<b>0.1911</b>	<b>0.00071</b>	<b>0.00025</b>
standard deviation	0.0018	0.0033	1.72e-05	6.27e-06
t-statistic	10.1	57.5	41.2	39.6

# Estimation results

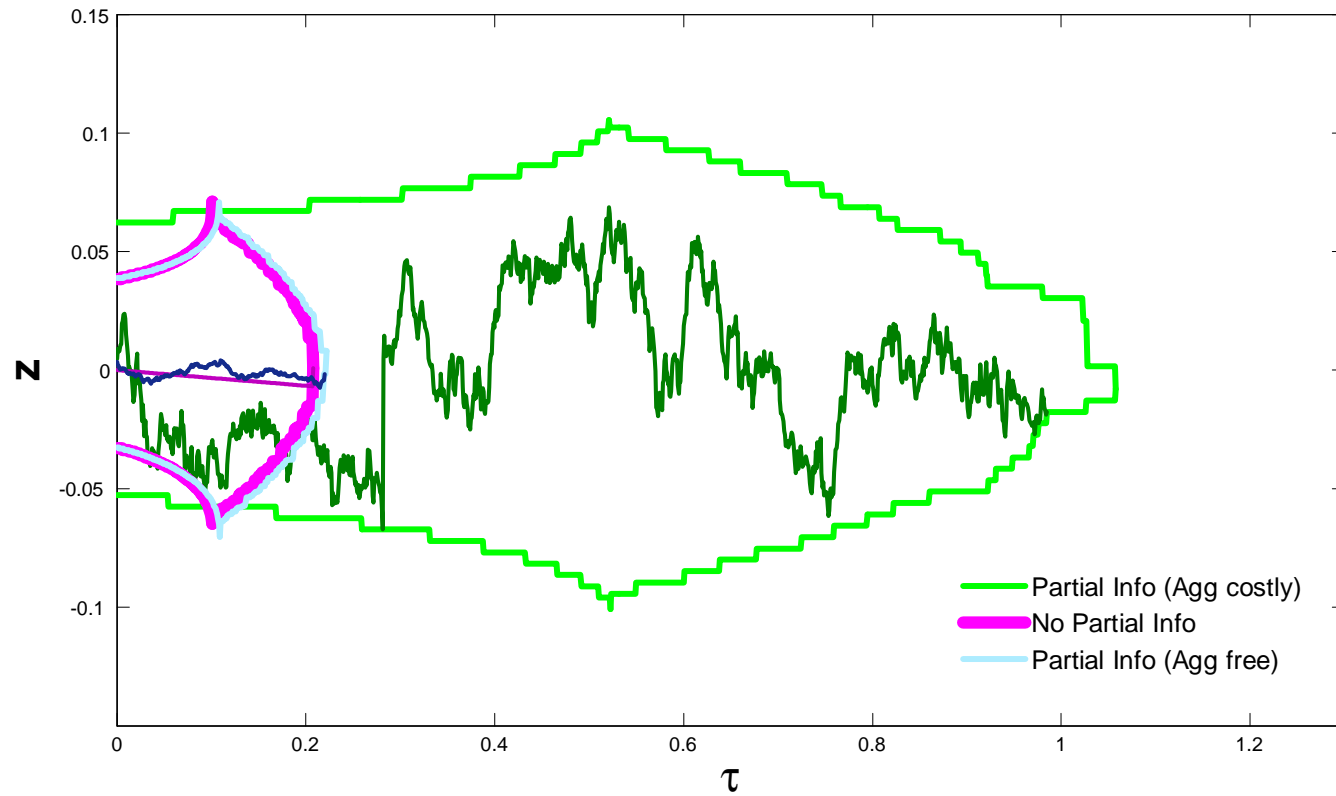
---

Target Statistics				
Statistic	$freq \Delta p > 0$	$freq \Delta p < 0$	$mean  \Delta p $	$median  \Delta p $
Data	0.1503	0.1152	0.0900	0.0710
No Partial	0.1465	0.1252	0.0953	0.0842
Partial $\sigma_a = \sigma_c$	0.1505	0.1227	0.0915	0.0788
Partial $\sigma_a = \sigma_f$	0.1477	0.1247	0.0949	0.0838

Target Statistics		
Statistic	$(fr \Delta p > 0)^2$	$std(freq \Delta p > 0)$
Data	0.0233	0.0263
No Partial	0.0221	0.0263
Partial $\sigma_a = \sigma_c$	0.0236	0.0297
Partial $\sigma_a = \sigma_f$	0.0231	0.0356

# Optimal rules implied by estimation

---



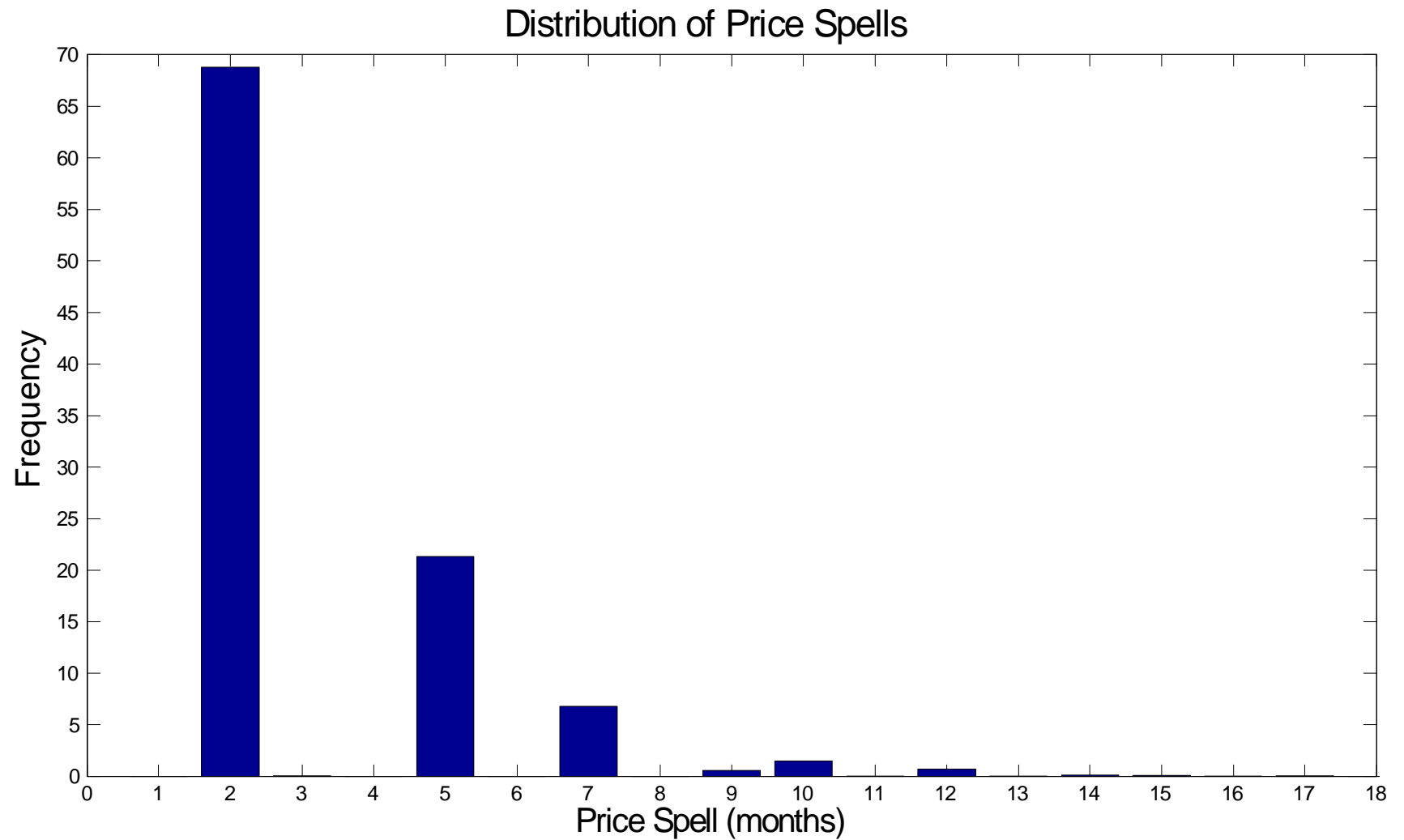
# Price setting results

---

Baseline	No Partial Info	Partial Info	Partial Info
		$(\sigma_a = \sigma_f)$	$(\sigma_a = \sigma_c)$
$K$	0.00024	0.00025	0.00076
$F$	0.00065	0.00071	0.00211
Adjustments per year	3.36	3.26	3.59
fully info. adj	100%	98%	25%
adj. without (full) info	0%	2%	75%
Information gatherings per year	4.88	4.64	1.37
resulting in immediate adj.	69%	69%	65%

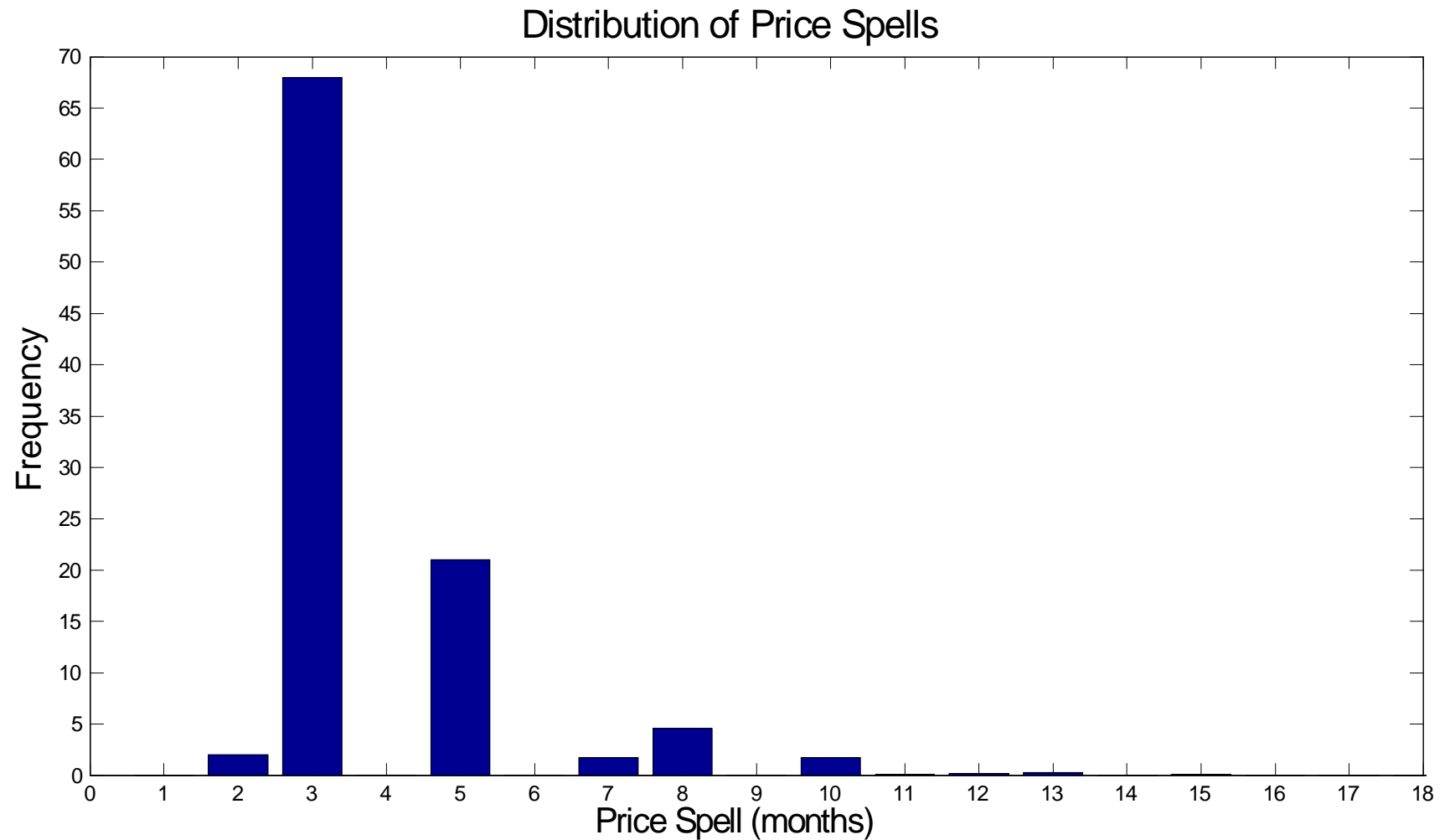
# Distribution of Price Spells No Partial Info

---



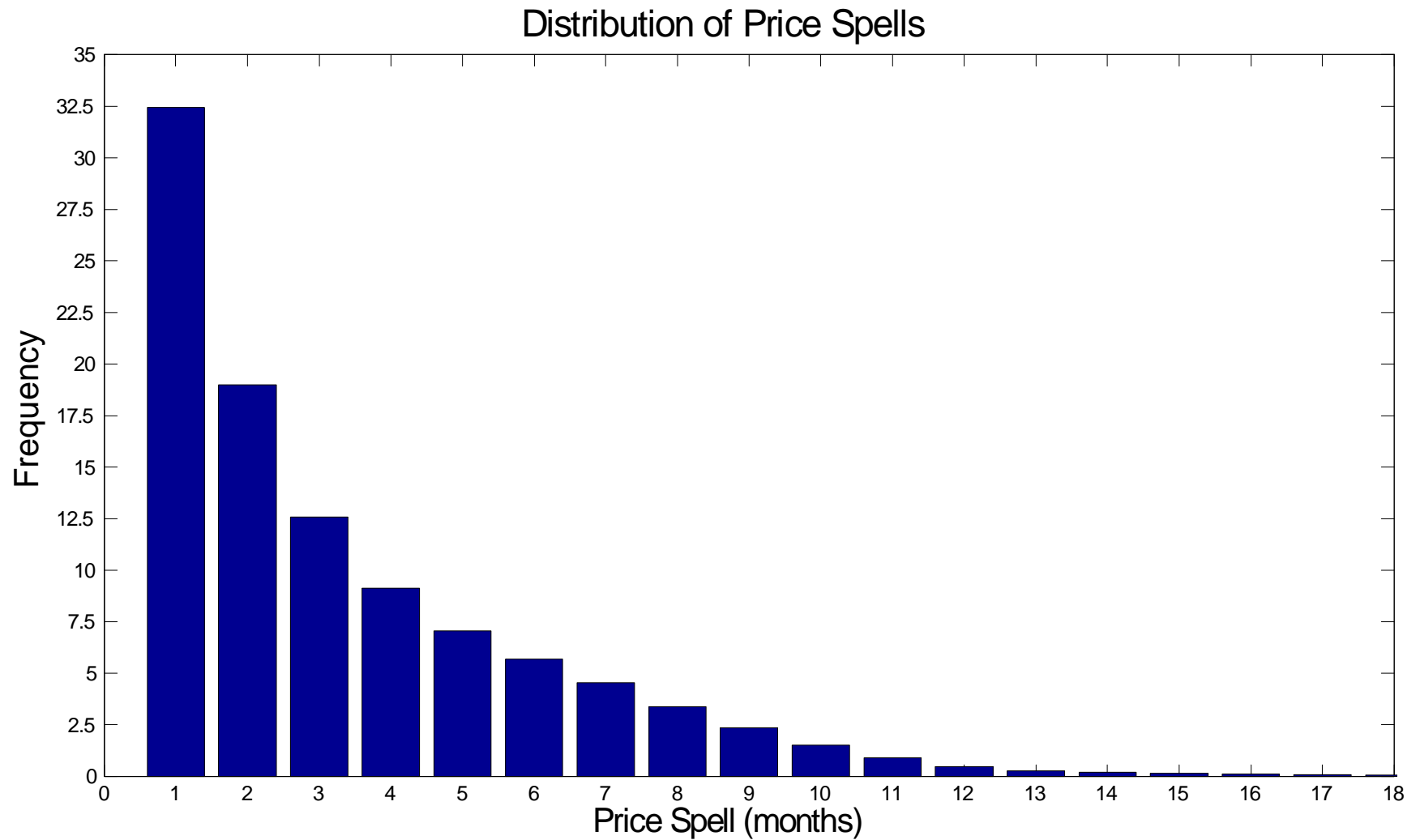
# Distribution of Price Spells Partial Info ( $\sigma_a = \sigma_f$ )

---



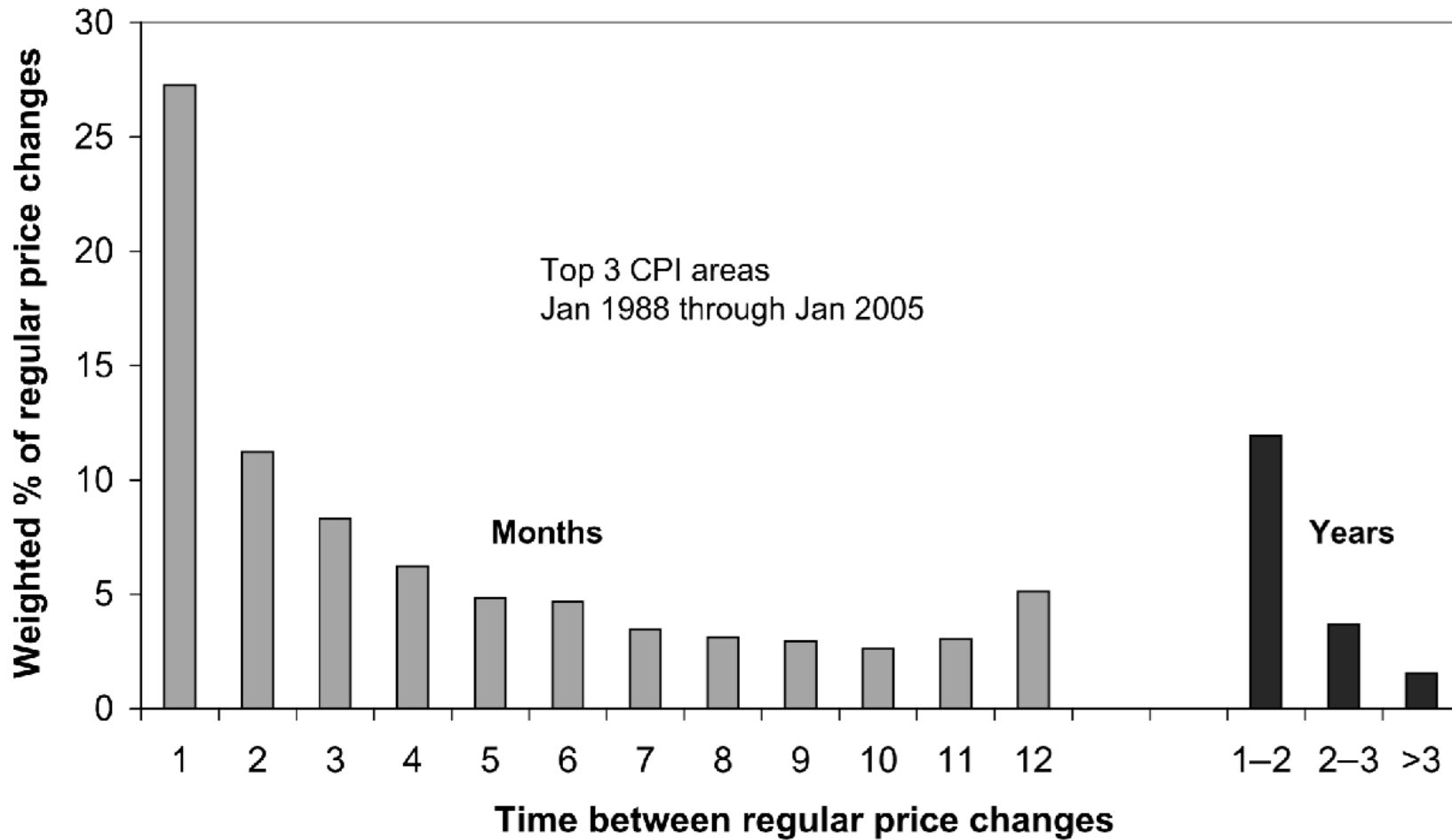
# Distribution of Price Spells Partial Info ( $\sigma_a = \sigma_c$ )

---



# Distribution of Price Spells in Klenow and Kryvtsov

---





# Effect of nominal aggregate demand shock in estimated economies

---

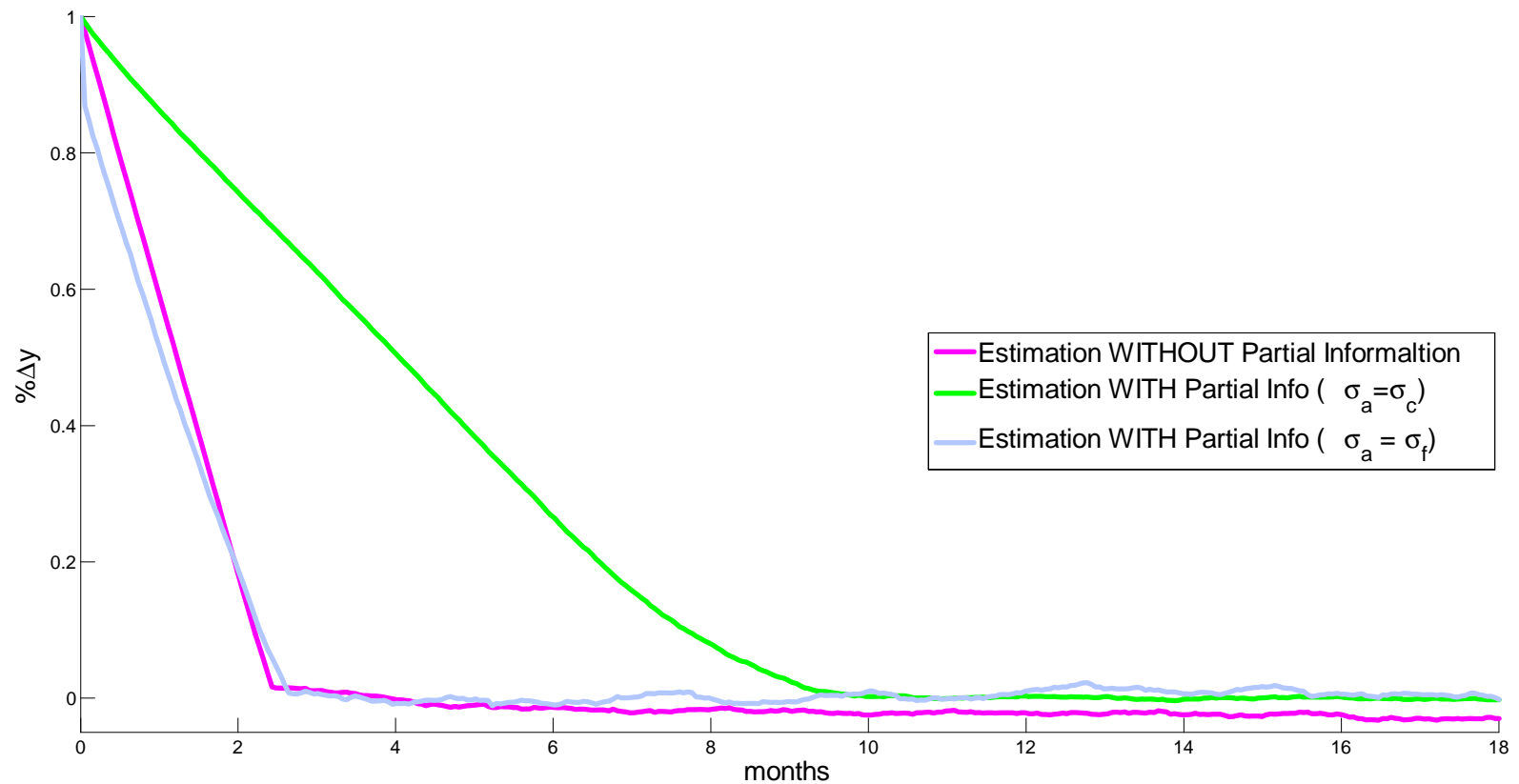
- Level of output is given by:

$$y_t = m_t - p_t$$

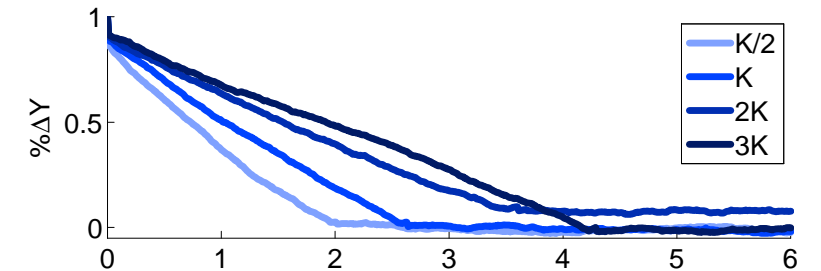
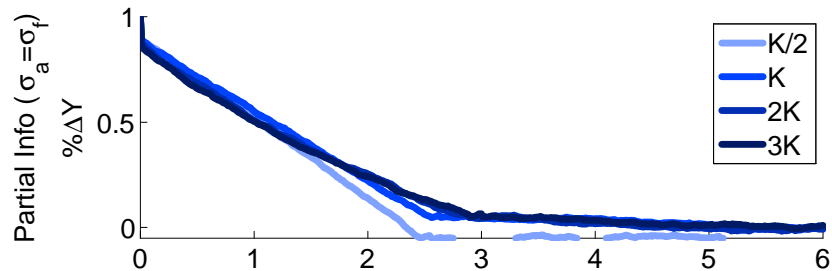
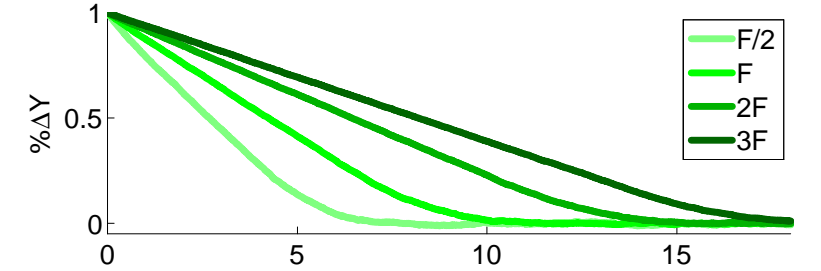
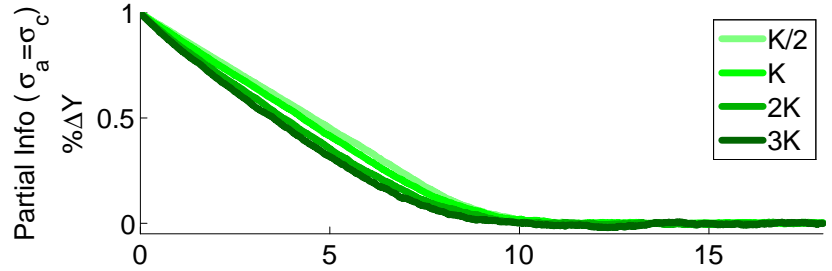
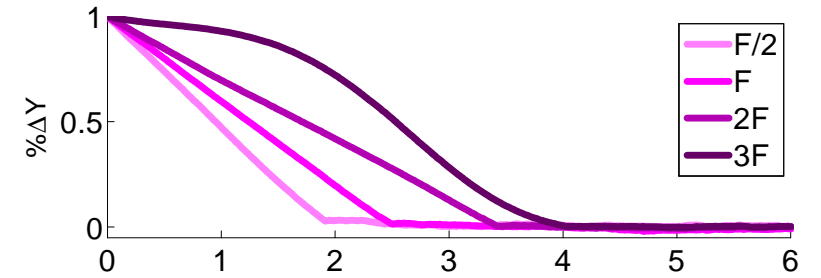
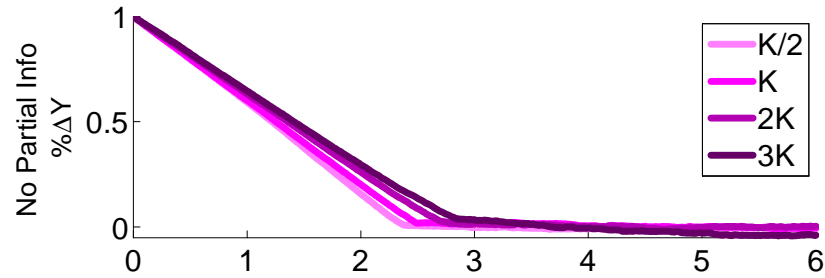
- Nominal aggregate demand  $m_t$  grows at rate  $\mu$
- After reaching the stochastic steady state:
  - 1% permanent increase in the level of nominal aggregate demand

# Effect of nominal aggregate demand shock in estimated economies

---



# Effect of aggregate demand shock: changing K and F



# Summing up

---

- New price setting model with costly price adjustment and partially costly information
  - price adjustments based on partial information
- Estimated partial information model with costly aggregate information:
  - fits price-setting statistics from micro data
  - generates realistic distribution of duration of price spells and
  - much larger monetary non-neutralities
- Helps reconcile empirical micro and macro evidence