

working
paper

9806

**Measuring the Rate
of Technological Progress
in Structures**

by Michael Gort, Jeremy Greenwood,
and Peter Rupert



FEDERAL RESERVE BANK OF CLEVELAND

Working Paper 9806

MEASURING THE RATE OF TECHNOLOGICAL PROGRESS IN STRUCTURES

by Michael Gort, Jeremy Greenwood, and Peter Rupert

Michael Gort is a professor of economics at the State University of New York at Buffalo; Jeremy Greenwood is a professor of economics at the University of Rochester; and Peter Rupert is an economist at the Federal Reserve Bank of Cleveland. This paper was prepared for a special issue of the *Review of Economic Dynamics* (edited by Per Krusell and Neil Wallace) honoring S. Rao Aiyagari. The authors thank Jennifer Ransom for her excellent research assistance.

Working papers of the Federal Reserve Bank of Cleveland are preliminary materials circulated to stimulate discussion and critical comment. The views stated herein are those of the author and are not necessarily those of the Federal Reserve Bank of Cleveland or of the Board of Governors of the Federal Reserve System.

Federal Reserve Bank of Cleveland working papers are distributed for the purpose of promoting discussion of research in progress. These papers may not have been subject to the formal editorial review accorded official Federal Reserve Bank of Cleveland publications.

Working papers are now available electronically through the Cleveland Fed's home page on the World Wide Web: <http://www.clev.frb.org>.

February 1998

Abstract

How much technological progress has been made in structures? This paper attempts to measure that progress using panel data on the age and rents for buildings. These data are interpreted according to a vintage capital model in which buildings are replaced with some chosen periodicity. There appears to have been significant technological advance in structures, which accounts for a major part of economic growth.

Measuring the Rate of Technological Progress in Structures

Michael Gort, Jeremy Greenwood, and Peter Rupert^{*†}

March 1998

Comments Welcome

Abstract

How much technological progress has there been in structures? An attempt is made to measure this using panel data on the age and rents for buildings. This data is interpreted through the eyes of a vintage capital model where buildings are replaced at some chosen periodicity. There appears to have been significant technological advance in structures that accounts for a major part of economic growth.

Keywords: Investment-specific technological progress; economic growth; vintage capital; replacement problem; economic depreciation; rent gradient.

^{*}*Affiliations:* Department of Economics, SUNY at Buffalo; Department of Economics, University of Rochester; Research Department, Federal Reserve Bank of Cleveland.

[†]This paper was prepared for a special issue of the *Review of Economic Dynamics* (edited by Per Krusell and Neil Wallace) honoring S. Rao Aiyagari. Jennifer Ransom is thanked for excellent research assistance. The latest version of this paper is kept at: <http://www.econ.rochester.edu/Faculty/Greenwood.html>

1. Introduction

So how much technological progress has there been in structures? Not much, might be the answer. Perhaps this answer should be reconsidered; because, as each decade passes new limits are reached in building airports, bridges, dams, highways, oil platforms, sea barriers, skyscrapers, stadiums, towers, and tunnels. Moreover, as new technology enables these advances, increased output per square foot of land is realized due to benefits such as faster and better communication and higher productivity resulting from more and better work space. Some examples may be in order to bolster this claim.

Skyscrapers: The Home Insurance Building is generally considered to be the world's first skyscraper. Built in Chicago in 1885 it was 10 stories tall. Compare this with Chicago's 110-story Sears towers completed in 1974. In less than 100 years the tallest building went from 10 to 100 floors. The 443 meter Sears Tower now plays second fiddle to the 452 meter Petronas Twin Towers in Kuala Lumpur built in 1997. The increase in building height reflects significant advances in engineering. While the Sears Towers are 200 feet taller than the Empire State Building (circa 1931) they weigh much less, 223,000 tons versus 365,000: a testimonial to better materials and design. Providing comfort to the occupants of a skyscraper is a major concern. For instance, the 29th floor is taken up by five chillers that cool the air in the building. Three of these weigh 5,000 tons a piece. Water that has been used in the chillers is pumped up 77 floors to four three-story high cooling towers located on levels 106 to 109. As the water cascades down the walls of the towers it is cooled by a huge fan. The tops of tall buildings are also subject to substantial movement from wind, causing motion sickness to the occupants.

To prevent this, two tuned dynamic dampers were installed in Boston's Hancock Tower (1969). Here, two three ton masses of lead are set on thin layers of oil on opposite ends of the 59th floor of the tower. They are connected to the structure with springs and shock absorbers. These dampers serve to mitigate the sway in the tower.

Suspension Bridges: The Brooklyn Bridge was a technological marvel when it opened in 1883. Its center span is 486 meters long. Contrast this to Japan's Akashi Kaikyo Bridge, opening in 1998, whose center span is 1990 meters long. The Messina Bridge planned for the year 2006 will connect mainland Italy with Sicily and will have a central span of 3300 meters. Long suspension bridges are very susceptible to the vicissitudes of nature, especially wind and water. Wind-excited vibrations at the natural frequency of the structure caused the collapse of the Tacoma Narrows suspension bridge in Puget Sound in 1940. To protect against oscillations, tuned mass dampers were added to the towers of Akashi Kaikyo Bridge, the first time in a bridge. These devices contain pendulums that rock in a direction opposite to the towers, thus dampening motion. This, together with other innovations, should allow the bridge to withstand winds up to 290 kilometers per hour.

Tunnels: The world's longest railway tunnel spans the Tsugaru Straits in Japan. Completed in 1988, it is 34 miles long and was dug through some of the most difficult rock ever encountered. The rock under the Tsugaru Straits is porous and unstable, permitting large water flows. So, before tunnelling, the rock had to be prepared. The fissures in the rock were sealed by pumping, under high pressure, a mixture of cement and a gelling agent into small holes that were drilled into the rock. Digging tunnels under water is dangerous. Once, during

construction, water flooded in at a rate of 80 tons per minute forcing a rapid evacuation. Even today, after the tunnel has been lined, without the aid of four pumping stations it would flood within 78 hours. Tunnelling has come a long way from the world's first railway tunnel, the 12.3 mile Simplon Tunnel built through the Alps between France and Italy, that opened in 1871.

Oil Platforms: At 630 feet tall and 824,000 metric tons it was the heaviest man-made object ever moved when it was hauled out to sea in 1981. This is taller than the United Nations Building and three times heavier than the World Trade Center. The Statfjord B oil platform was a mammoth undertaking. One hundred miles from shore with 200 people aboard, it needs to be able to withstand the worst of weather. In waves of 100 feet and in wind of 100 miles per hour it is designed to shift less than one half of an inch. It can produce 150,000 barrels of oil a day.

So again, how much technological progress has there been in structures? The answer here is that the rate of technological progress in structures is about 1.8% per year, and accounts for 32% of economic growth. The method of estimating technological progress employed here differs significantly from current growth accounting practice. First, price data is used to shed information on technological progress. Gordon's (1990) data on the price for new producer durable equipment shows that there has been a substantial secular decline in the relative price of new equipment over the postwar period.¹ In constructing his price index, Gordon (1990) attempts to control for the operating characteristics of equipment that are important for production. This suggests that there has been significant techno-

¹Greenwood, Hercowitz and Krusell (1997) use Gordon's (1990) prices to calculate how much of postwar economic growth was due to equipment-specific technological progress.

logical progress in the production of new equipment. Likewise, a panel data set of buildings used in the current analysis shows that new structures rent for more than old ones. To the extent that new buildings have new and improved technology embodied in their structures, this rent gradient will reflect technological progress, *ceteris paribus*.

Second, a general equilibrium approach to growth accounting is taken. This allows for a tight linkage to be drawn between the observed rent gradient for buildings and the rate of technological progress in structures. Furthermore, conventional growth accounting uses an aggregate production function to decompose output growth into technological progress and changes in inputs. Clearly, though, a large part of the growth in equipment and structures is due to technological progress. The general equilibrium approach taken here allows for the growth in output due to capital accumulation to be broken down to its underlying sources of technological progress. Last, in a world where technological progress may be embodied in the form of new equipment and structures, conventional measures of capital stocks become suspect. The issue is how to aggregate the new and improved capital with the old capital. To the extent that technological progress in the production of new capital is neglected, these measures will underestimate the true growth in the stocks of physical capital. As a consequence, investment-specific technological progress is mismeasured, leading to an overestimate of the contribution of neutral technological progress to economic growth. The use of these measures is avoided here.

2. Theory

2.1. Environment

Production is undertaken at a fixed number of locations, distributed uniformly on the unit interval, and requires the use of three inputs: equipment, structures, and labor. Each location has associated with it a stock of structures of a certain age or vintage. The manager of a location must decide at each point in time whether to replace this stock of structures or not. Equipment and labor can be hired each period on a spot market. Let production at a location using structures of vintage j be given by

$$o(j) = zk_e(j)^{\alpha_e} k_s(j)^{\alpha_s} l(j)^{\beta}, \quad (2.1)$$

where z is the economy-wide level of total factor productivity and $k_e(j)$, $k_s(j)$, and $l(j)$ are the inputs of equipment, structures and labor. Denote the number of locations using structures of vintage j by $p(j)$ and let the oldest age of structures be T . Then $\int_0^T p(j) dj = 1$. Aggregate output is thus

$$y = \int_0^T p(j) zk_e(j)^{\alpha_e} k_s(j)^{\alpha_s} l(j)^{\beta} dj. \quad (2.2)$$

Output can be used for three purposes: consumption, c , investment in equipment, i_e , and investment in structures, i_s . Hence

$$c + i_e + i_s = y. \quad (2.3)$$

Imagine constructing a new building at some location. Suppose that a unit of forgone consumption can purchase v new units of structures. Then, building $k_s(0)$ units of new structures would cost $k_s(0)/v$ units of consumption. Let v grow at rate γ_v ; this denotes structure-specific technological progress. Aggregate gross

investment in structures will therefore read

$$i_s = p(0)k_s(0)/v. \quad (2.4)$$

Structures remain standing until they are replaced. While structures suffer no physical depreciation, they must be maintained. Let the initial maintenance cost be a fraction $\mu(0)$ of the building's purchase price. These costs grow exogenously at rate $\gamma_\mu + \gamma_y$ as the building ages, where γ_y is the economy's growth rate. The question of interest here is: When should a building be replaced?

Equipment is mobile and can be freely rented on an economy-wide equipment market. The law of motion for equipment has the form

$$\frac{dk_e}{dt} = -\delta_e k_e + q i_e, \quad (2.5)$$

The variable q represents equipment-specific technological progress. This occurs over time at rate γ_q . The rate of physical depreciation on equipment is δ_e .

2.2. The Location Manager's Decision

2.2.1. Static Profit Maximization

At a point in time the manager of a location should hire equipment and labor to maximize the location's profits, given his stock of structures. Consider the static profit-maximizing decision at a location using vintage- j structures:

$$\pi(j) = \max_{k_e(j), l(j)} \{z k_e(j)^{\alpha_e} k_s(j)^{\alpha_s} l(j)^\beta - r_e k_e(j) - w l(j)\}, \quad \text{P(1)}$$

where r_e is the economy-wide rental price for equipment and w is the wage rate. The first-order conditions are

$$\alpha_e z k_e(j)^{\alpha_e - 1} k_s(j)^{\alpha_s} l(j)^\beta = r_e, \quad (2.6)$$

and

$$\beta z k_e(j)^{\alpha_e} k_s(j)^{\alpha_s} l(j)^{\beta-1} = w. \quad (2.7)$$

By multiplying (2.6) by $k_e(j)$ and (2.7) by $l(j)$ it is easy to establish from P(1) that

$$\pi(j) = (1 - \alpha_e - \beta) z k_e(j)^{\alpha_e} k_s(j)^{\alpha_s} l(j)^{\beta}.$$

Next, observe that (2.6) and (2.7) imply that

$$k_e(j) = \frac{\alpha_e}{\beta} \frac{w}{r_e} l(j), \quad (2.8)$$

and

$$l(j) = \left[\frac{\beta^{1-\alpha_e} \alpha_e^{\alpha_e} z (1/r_e)^{\alpha_e} k_s(j)^{\alpha_s}}{w^{1-\alpha_e}} \right]^{\frac{1}{1-\alpha_e-\beta}}, \quad (2.9)$$

so that rents at a point in time (the return to the fixed factor, here land) can be expressed as

$$\pi(j) = (1 - \alpha_e - \beta) z^{\frac{1}{1-\alpha_e-\beta}} \alpha_e^{\frac{\alpha_e}{1-\alpha_e-\beta}} \beta^{\frac{\beta}{1-\alpha_e-\beta}} r_e^{\frac{-\alpha_e}{1-\alpha_e-\beta}} w^{\frac{-\beta}{1-\alpha_e-\beta}} k_s(j)^{\frac{\alpha_s}{1-\alpha_e-\beta}}. \quad (2.10)$$

The profits from each location, net of any repair and maintenance costs and investment in structures, are rebated to consumers each period.

2.2.2. The Replacement Problem

When should the manager of a location replace the structures on his site? Suppose that at date 0 the manager has $k_{s,0}(0)$ units of new structures.² At what date T should he replace his building and how much should his investment in new

²Time is indicated by subscripts. So for example, $k_{s,t}(j)$ indicates the amount of age- j structures at time t .

structures, $k_{s,T}(0)$, be at that time? Clearly, he should choose these variables to maximize the value of the location as denoted by $V(k_{s,0}(0))$. The manager's date-0 problem can be written as

$$V(k_{s,0}(0)) = \max_{k_{s,T}(0), T} \left\{ \int_0^T [\pi_t(t) - \mu(t)k_{s,0}(0)/v_0] e^{-\iota t} dt + e^{-\iota T} [V(k_{s,T}(0)) - k_{s,T}(0)/v_T] \right\}, \quad \text{P(2)}$$

where ι represents the time-invariant interest rate. The solution dictates that

$$[\pi_T(T) - \mu(T)k_{s,0}(0)/v_0] - \iota[V(k_{s,T}(0)) - k_{s,T}(0)/v_T] = 0, \quad (2.11)$$

and

$$V_{k_s}(k_{s,T}(0)) = 1/v_T. \quad (2.12)$$

2.3. Equipment Rentals

At each point in time the equipment manager has k_e units of equipment that he can rent out at r_e . He must decide how much to invest, i_e , in new equipment. This investment can be financed at the fixed interest rate ι . The optimal control problem governing the accumulation of equipment is summarized by the current-value Hamiltonian shown below and its associated efficiency conditions.

$$\begin{aligned} \mathcal{H} &= r_e k_e - i_e + \lambda[i_e q - \delta_e k_e], \\ \mathcal{H}_{i_e} &= -1 + \lambda q = 0, \end{aligned} \quad (2.13)$$

and

$$d\lambda/dt = \iota\lambda - \mathcal{H}_{k_e} = \iota\lambda - r_e + \lambda\delta_e. \quad (2.14)$$

Observe that from (2.13) that $\gamma_\lambda = -\gamma_q$ so that (2.14) can be expressed as

$$r_e = (\iota + \delta_e + \gamma_q)/q. \quad (2.15)$$

This gives the rental price for equipment. This formula has a simple interpretation. A unit of forgone consumption can purchase q units of equipment that will rent for $r_e q$. This rental income must cover the forgone interest, ι , physical depreciation, δ_e , and the capital loss, γ_q , induced by the fact the price of equipment (in terms of consumption) is falling across time.³

2.4. The Representative Consumer's Problem

Let a consumer's lifetime utility function be given by

$$\int_0^\infty \ln c_t e^{-\rho t} dt.$$

Now, the consumer is free to lend in terms of bonds, a , earning the return ι . In addition to the interest he realizes on his lending activity, the consumer earns labor income, w , and the profits from his locations (net of any repair and maintenance costs and investment in structures), $\int_0^T p(j)\pi(j)dj - p(0)k_s(0)/v$. The law of motion governing his asset accumulation reads

$$da/dt = w + \int_0^T p(j)[\pi(j) - \mu(j)k_s(j)e^{\gamma_s j}/v]dj - p(0)k_s(0)/v + \iota a.$$

The efficiency condition governing asset accumulation is

$$\frac{1}{c} \frac{dc}{dt} = (\iota - \rho), \tag{2.16}$$

which states the familiar condition that consumption should grow at the rate at which the interest rate exceeds the rate of time preference.

³A unit of equipment sells for $1/q$ units of consumption, and this price is falling over time at rate γ_q .

2.5. Market Clearing Conditions

At each point in time the markets for labor and bonds must clear. Consequently,

$$\int_0^T p(j)l(j)dj = 1. \quad (2.17)$$

and

$$\int_0^T p(j)k_e(j)dj = qa.$$

2.6. Balanced Growth

The balanced growth path will be uncovered using a guess and verify procedure. To this end, conjecture that along a balanced growth path consumption, investment in equipment and structures, aggregate output, and the stocks of equipment and structures at a location of any given age, will all be growing at constant rates. Likewise, it seems reasonable to believe that the age distribution of structures and the amount of labor allocated to an age- j location will be constant through time. If so, equation (2.2) then implies that along a balanced growth path output will grow at rate

$$\gamma_y = \gamma_z + \alpha_e \gamma_e + \alpha_s \gamma_s, \quad (2.18)$$

where $\gamma_y \equiv (1/y)dy/dt$, $\gamma_z \equiv (1/z)dz/dt$, $\gamma_e \equiv [1/k_e(j)]dk_e(j)/dt$, and $\gamma_s \equiv [1/k_s(j)]dk_s(j)/dt$. Additionally, from the resource constraint (2.3), consumption, equipment investment, and structure investment will all need to grow at the same rate as output, or would disappear relative to output. Consumption growing at the fixed rate γ_y requires that the interest rate remains constant at

$$\iota = \rho + \gamma_y, \quad (2.19)$$

a fact evident from (2.16).

Next, note that the law of motion for equipment in balanced growth reads

$$\gamma_e = -\delta_e + \frac{qi_e}{k_e}.$$

Thus, γ_e can be constant if and only if qi_e/k_e is too. This can only be true when

$$\gamma_e = \gamma_q + \gamma_y, \quad (2.20)$$

Analogously, $i_s/y = [p(0)k_s(0)/v]/y$ can only remain fixed if

$$\gamma_s = \gamma_v + \gamma_y, \quad (2.21)$$

where, as must be obvious by now, $\gamma_q \equiv (1/q)dq/dt$ and $\gamma_v \equiv (1/v)dv/dt$.

The rate of growth in output, as a function of the underlying sources of technological progress, can now be uncovered by substituting (2.20) and (2.21) into (2.18) to obtain

$$\gamma_y = \frac{1}{1 - \alpha_e - \alpha_s} \gamma_z + \frac{\alpha_e}{1 - \alpha_e - \alpha_s} \gamma_q + \frac{\alpha_s}{1 - \alpha_e - \alpha_s} \gamma_v. \quad (2.22)$$

In turn, using this in (2.20) and (2.21) gives

$$\gamma_e = \frac{1}{1 - \alpha_e - \alpha_s} \gamma_z + \frac{1 - \alpha_s}{1 - \alpha_e - \alpha_s} \gamma_q + \frac{\alpha_s}{1 - \alpha_e - \alpha_s} \gamma_v, \quad (2.23)$$

and

$$\gamma_s = \frac{1}{1 - \alpha_e - \alpha_s} \gamma_z + \frac{\alpha_e}{1 - \alpha_e - \alpha_s} \gamma_q + \frac{1 - \alpha_e}{1 - \alpha_e - \alpha_s} \gamma_v. \quad (2.24)$$

Equation (2.22) is the key for opening the door to growth accounting. Not surprisingly, the contribution of equipment-specific technological progress to economic growth will be larger the bigger is equipment's share of income, α_e , relative to that of the nonreproducible factors, $1 - \alpha_e - \alpha_s$. The contribution of structure-specific

technological progress to growth depends in a similar way on structure's share of income, α_s . Observe that stocks of equipment and structures grow at a faster rate than output, since $\alpha_e < 1 - \alpha_s$ and $\alpha_s < 1 - \alpha_e$.

Next, it is easy deduce from (2.15) and (2.7) that the factor prices r_e and w will grow at rates

$$\gamma_{r_e} = -\gamma_q,$$

and

$$\gamma_w = \gamma_y.$$

By using the above two conditions, in conjunction with (2.22), in (2.10), it is easy to show that, *when the stock of structures is held fixed*, profits on a building will rise over time at rate

$$\begin{aligned} \gamma_\pi &= \left(\frac{1 - \alpha_e - \alpha_s - \beta}{1 - \alpha_e - \beta}\right)\left(\frac{1}{1 - \alpha_e - \alpha_s}\right)\gamma_z + \left(\frac{1 - \alpha_e - \alpha_s - \beta}{1 - \alpha_e - \beta}\right)\left(\frac{\alpha_e}{1 - \alpha_e - \alpha_s}\right)\gamma_q \\ &\quad - \left(\frac{\beta}{1 - \alpha_e - \beta}\right)\left(\frac{\alpha_s}{1 - \alpha_e - \alpha_s}\right)\gamma_v \\ &< \gamma_y. \end{aligned} \tag{2.25}$$

Observe that profits grow at a rate less than output. This, together with rising maintenance costs, motivates the replacement of buildings. The location manager's replacement decision is driven by the lure of profits. For a given stock of structures, profits are forever being squeezed by rising labor costs. To increase these dwindling profits the manager must replace his old structure with a new and improved building.

Now, consider the economy's cross section of buildings at a point in time. It is easy to calculate from (2.10) that the percentage change in rents as a function

of age, or the rent gradient δ_s , should be given by

$$\delta_s = -\frac{\alpha_s}{1 - \alpha_e - \beta}\gamma_s, \quad (2.26)$$

since the stock of structures declines at rate γ_s as a function of age (while factor prices remain constant). This formula plays a starring role in the analysis. It is a measure of obsolescence in buildings. In the absence of depreciation, a new building rents for more than an old one only because it offers more efficiency units of structures.

Along a balanced growth path the profits of an age- j building will grow at rate γ_y , a fact readily apparent from (2.10). Since T is constant it then follows that $V(k_{s,0}(0)) = e^{-\gamma_y T} V(k_{s,T}(0))$. Furthermore, note that $k_{s,0}(0)/v_0 = e^{-\gamma_y T} k_{s,T}(0)/v_T$. This allows the first-order condition (2.11) to be written as

$$[e^{\gamma_\pi T} \pi_0(0) - e^{(\gamma_\mu + \gamma_y)T} \mu(0) k_{s,0}(0)/v_0] - \iota e^{\gamma_y T} [V(k_{s,0}(0)) - k_{s,0}(0)/v_0] = 0, \quad (2.27)$$

where everything has now been expressed in terms of date-0 values. From P(2) it is easy to calculate that

$$\begin{aligned} V(k_{s,0}(0)) &= \frac{\pi_0(0) \int_0^T e^{-(\iota - \gamma_\pi)t} dt - \mu(0) [k_{s,0}(0)/v_0] \int_0^T e^{-(\iota - \gamma_\mu - \gamma_y)t} dt}{1 - e^{-(\iota - \gamma_y)T}} \\ &\quad - \frac{e^{-(\iota - \gamma_y)T} k_{s,0}(0)/v_0}{1 - e^{-(\iota - \gamma_y)T}} \\ &= \frac{\pi_0(0) [1 - e^{-(\iota - \gamma_\pi)T}]/(\iota - \gamma_\pi)}{1 - e^{-(\iota - \gamma_y)T}} - \frac{e^{-(\iota - \gamma_y)T} k_{s,0}(0)/v_0}{1 - e^{-(\iota - \gamma_y)T}} \\ &\quad - \frac{\mu(0) [k_{s,0}(0)/v_0] [1 - e^{-(\iota - \gamma_\mu - \gamma_y)T}]/(\iota - \gamma_\mu - \gamma_y)}{1 - e^{-(\iota - \gamma_y)T}}. \end{aligned} \quad (2.28)$$

Likewise, from P(2) it is easy to see that in balanced growth

$$V_{k_s}(k_{s,0}(0)) = \frac{[1 - e^{-(\iota - \gamma_\pi)T}] \pi_{k_s,0}(0)}{(\iota - \gamma_\pi)} - \frac{[1 - e^{-(\iota - \gamma_\mu - \gamma_y)T}] \mu(0)}{(\iota - \gamma_\mu - \gamma_y)}, \quad (2.29)$$

where

$$\pi_{ks,0}(0) = \alpha_s z^{\frac{1}{1-\alpha_e-\beta}} \alpha_e^{\frac{\alpha_e}{1-\alpha_e-\beta}} \beta^{\frac{\beta}{1-\alpha_e-\beta}} r_{e,0}^{\frac{-\alpha_e}{1-\alpha_e-\beta}} w_0^{\frac{-\beta}{1-\alpha_e-\beta}} k_{s,0}(0)^{\frac{\alpha_e+\alpha_s+\beta-1}{1-\alpha_e-\beta}}, \quad (2.30)$$

so that the first-order condition will read

$$V_{k_s}(k_{s,0}(0)) = 1/v_0. \quad (2.31)$$

The model is almost complete except that the date-0 market clearing wage rate needs to be computed. The age distribution of structures over locations will be uniformly distributed on the interval $[0, T]$. The labor market clearing condition (2.17) can accordingly be rewritten as $(1/T) \int_0^T l(j) dj = 1$. Substituting (2.9) into this condition and using the fact that $k_{s,0}(j) = k_{s,0}(0)e^{-\gamma_s j}$ yields

$$\begin{aligned} w_0 &= [\beta^{1-\alpha_e} \alpha_e^{\alpha_e} z_0 (\frac{1}{r_{e,0}})^{\alpha_e} k_{s,0}(0)^{\alpha_s}]^{1/(1-\alpha_e)} \\ &\times [\frac{1 - e^{-T\alpha_s\gamma_s/(1-\alpha_e-\beta)}}{T\alpha_s\gamma_s/(1-\alpha_e-\beta)}]^{(1-\alpha_e-\beta)/(1-\alpha_e)}. \end{aligned} \quad (2.32)$$

The solution to the model's balanced growth path is now completely characterized. To see this note that equations (2.10), (2.15), (2.19), (2.22), (2.24), and (2.27) to (2.32) represent a system of 11 equations in the 11 unknowns $\pi_0(0)$, ι , $r_{e,0}$, γ_y , γ_s , T , $V(k_{s,0}(0))$, $V_{k_s}(k_{s,0}(0))$, $\pi_{ks,0}(0)$, $k_{s,0}(0)$, and w_0 .⁴

Last, it was stated that the replacement of structures was driven by the lure for profits. For a given stock of structures, profits are squeezed over time for two reasons: rising real wages and maintenance costs. To see the important role that profits play in replacement, assume that there are no profits, because production is governed by constant returns to scale, and that buildings can be maintained cost free. It is easy to deduce that in this situation structures will never be replaced.

⁴Equations (2.10) and (2.15) at time zero read $\pi_0(j) = (1 - \alpha_e - \beta) z_0^{\frac{1}{1-\alpha_e-\beta}} \alpha_e^{\frac{\alpha_e}{1-\alpha_e-\beta}} \beta^{\frac{\beta}{1-\alpha_e-\beta}} r_{e,0}^{\frac{-\alpha_e}{1-\alpha_e-\beta}} w_0^{\frac{-\beta}{1-\alpha_e-\beta}} k_{s,0}(j)^{\frac{\alpha_s}{1-\alpha_e-\beta}}$ and $r_{e,0} = (\iota + \delta_e + \gamma_q)/q_0$.

Proposition 2.1. *(No Replacement): If $\alpha_e + \alpha_s + \beta = 1$ and $\mu(0) = 0$ then $T = \infty$.*

Proof. Observe that in this situation $\pi_{k_s,0}(0)k_{s,0}(0) = \pi_0(0)$, since $1 - \alpha_e - \beta = \alpha_s$. Using (2.28) and (2.29) this then implies that $V_{k_s}(k_{s,0}(0))k_{s,0}(0) = V(k_{s,0}(0))$ so that $V(k_{s,0}(0)) = k_{s,0}(0)/v_0$. The righthand side of (2.27) will therefore always be strictly positive so that there does not exist a finite T satisfying this equation. Hence, in balanced growth path it must transpire that $T = \infty$. ■

3. Measurement

3.1. Estimation

There are three parameters that need to be estimated — the rent gradient, δ_s , maintenance costs for newer buildings, ϕ , and the growth rate in maintenance costs, γ_μ . To do this, we obtained data from the Building Owners and Managers Association International (BOMA). The data used for the estimation is based on a panel covering approximately 200 office buildings across the United States from 1988 to 1996.⁵ The data set includes information on age, location, size, rent, and several categories of expenses. Summary statistics for the sample are given in Table 1.

⁵This data was assembled by BOMA International with the names and addresses removed.

Table 1				
variable	mean	std. dev.	minimum	maximum
square feet	312,403	330,065	15,683	2,529,269
repair and main./s.f. (1996)	\$1.42	\$0.776	\$0.353	\$5.40
rent/s.f. (1996)	\$15.23	\$6.93	\$1.52	\$56.6
age	25.9	22.2	2	128
floors	16.0	13.4	2	80

The average size building is 312,043 sq. ft.; the smallest being 15,683 sq. ft. and the largest 2,529,269 sq. ft. The oldest building was built in 1866 and the newest 1987. (Each buildings was in every year of the 9-year sample).

Figure 3.1 plots the kernel estimate of (the log of) rent per square foot as a function of age. As can be seen in the figure, the decline in rent is monotonically decreasing until the building is approximately 50 years old. Then there is a sharp increase, returning to a monotonic decline a few years later. This may reflect extensive remodelling or refurbishing of a building. To the extent that this is the case, it could in essence be considered a new or different building. Therefore, the estimating equation is based on a restricted sample of those buildings 52 years old or younger. Figure 3.2 plots the kernel estimate of (the log of) repair and maintenance as a function of age. Repair and maintenance costs rise over time.

Given that the data set contains observations on the same buildings over time, a fixed effects estimator is used to determine the value for the rent gradient, δ_s . The final specification also includes the log of real repair and maintenance expenditures. If repair and maintenance expenditures counteracted the effects of physical wear and tear, then the coefficient on age in the regression captures the



Figure 3.1:

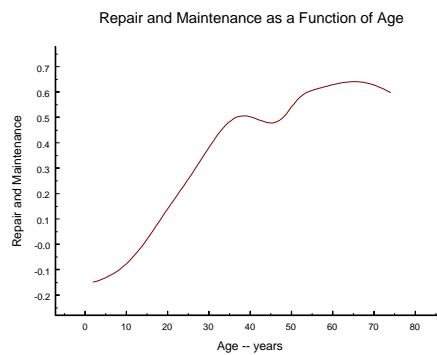


Figure 3.2:

effect of depreciation due to obsolescence alone⁶. Due to the fact that a fixed effects estimator is used, estimates cannot be obtained for things such as regional location, or whether the building is located downtown or in the suburbs, as these are also fixed over time for an individual building.

The results for δ_s are given in Table 2.

Table 2	
	Fixed effect
variable	regression
constant	3.05
	(0.041)
age	-0.023
	(0.002)
rep. & maint.	0.099
	(0.028)

The value of ϕ was chosen to represent the ratio of repair and maintenance to rents in newer buildings. From the data the number for buildings 5 years old or younger was calculated. The value of ϕ is 0.055. To obtain a parameter estimate for γ_μ a fixed effects estimator was also used, again with age as the explanatory variable; the results are presented in Table 3.⁷

⁶Experiments with regressions not including expenditures on repair and maintenance were also performed; however, they did not differ substantially from those reported in the tables.

⁷The fact that expenditures on repair and maintenance begin to decline with age suggests that such expenditures may be endogenous, i.e., at some point less and less is spent, and the building is allowed to deteriorate. Therefore, the estimation is based on the sample where

Table 3	
	Fixed effect
variable	regression
constant	-0.157
	(0.037)
age	0.010
	(0.003)

3.2. Calibration

The model's parameters are assigned either (i) on the basis a priori information about their values or (ii) so that the model's balanced growth is consistent with certain features displayed in the U.S. data over the postwar period.

3.2.1. A Priori Information

1. $\gamma_q = 0.32$. This number represents the average annual decline in the relative price of equipment price for the postwar period based on data taken from Gordon (1990).⁸
2. $\delta_e = 0.12$. This is an estimate of average depreciation rate for equipment used in constructing NIPA's equipment stock figures.⁹

expenditures are increasing, since the maintained assumption is that this is the amount it would take to keep the building in its original condition. Note that since expenditures are increasing over time it costs more each year to keep up the building.

⁸As computed by Greenwood, Hercowitz and Krusell (1997).

⁹Again, as calculated by Greenwood, Hercowitz and Krusell (1997).

3. $\beta = 0.68$. Labor's share of income, as estimated from the NIPA for the period 1959-1996. Here labor income is defined as total compensation of employees in nominal terms. Income is taken to be nominal GDP minus nominal gross housing product.
4. $\phi = 0.055$. This is the estimate from Section 3.1
5. $\gamma_\mu = 0.010$. Again, as estimated from Section 3.1.

3.2.2. Restrictions on Balanced Growth

Parameter values still need to be determined for α_e , α_s , $\mu(0)$, γ_v , γ_z and ρ . These six parameters will be pinned down using six long-run restrictions from the data.

1. Over the postwar period 1959-1996 output-per-manhour worked in the U.S. economy has grown at an average rate of 1.22%. Again, nominal output is measured as nominal GDP minus nominal gross housing product. Since the numeraire in the model was consumptions goods, this series was divided through by the implicit price deflator for personal consumption expenditures on nondurables and nonhousing services. Total private sector manhours was calculated as an annual average of average weekly hours of total private production or nonsupervisory workers multiplied by the number of civilians employed. If the model is to be consistent with this fact, then

$$\gamma_y = 0.0122. \tag{3.1}$$

2. In the U.S. the equipment-investment-to-GDP ratio averaged 7.3% for the period 1959-1996. Using the law of motion for equipment it is easy to see

that in balanced growth date-0 investment in equipment is given by $i_{e,0} = (\gamma_y + \gamma_q + \delta_e)k_{e,0}/q_0$. Now, from (2.8) it is apparent that $k_{e,0} = \int p(j)k_{e,0}(j)dj = (\alpha_e w)/(\beta r_{e,0}) \int l(j)dj = (\alpha_e w)/(\beta r_{e,0})$ (since the supply of labor is one). Finally, date-0 GDP is given by w_0/β . Hence, the following restriction on the model's balanced growth path obtains:

$$\frac{i_e}{y} = \frac{\alpha_e}{r_{e,0}} = 0.073. \quad (3.2)$$

3. The ratio of structure investment to GDP in the U.S. economy is 4.1% (for the 1959-1996 sample period). If this restriction is imposed on the model then

$$\frac{i_s}{y} = \frac{[k_s(0)/v_0]/T}{w_0/\beta} = 0.041. \quad (3.3)$$

In a world with investment-specific technological progress conventional measures of capital stocks are flawed since adjusting for quality improvements is difficult. Therefore, measures of $(k_e/q)/y$ and $(k_s/v)/y$ taken from NIPA are likely to be unreliable. Nominal investments, however, do not suffer from this problem so that i_e/y and i_s/y can be measured with reasonable accuracy.

4. The average age of buildings in the sample is 26 years. Now, recall that the lure of profits was a central factor in the firm's replacement decision. Thus, the returns to scale, as given by α_e and α_s , should be critical in determining T . The following restriction on the average age of buildings is added to the model's balanced growth path:

$$\frac{1}{T} \int_0^T j dj = \frac{T}{2} = 26. \quad (3.4)$$

5. In Section 3.1 it was found that the average ratio of repair and maintenance to rents in newer buildings is 0.055. This dictates the following condition on $\mu(0)$:

$$\mu(0) = 0.055 \times \frac{\pi_0(0)v_0}{k_{s,0}(0)}. \quad (3.5)$$

6. The estimation results from Section 3.1 show that a one year increase in a building's age reduces its rent by 2.3%. Recall that the rent gradient is a measure of obsolescence of structures. Hence, it should provide useful information for calculating γ_v . Using the rent gradient formula (2.26), together with (2.24), leads to the last restriction.

$$\gamma_v = \frac{(1 - \alpha_e - \beta)}{\alpha_s} \delta_s - \gamma_y = \frac{(1 - \alpha_e - \beta)}{\alpha_s} \times 0.023 - \gamma_y. \quad (3.6)$$

Counting establishes that equations (2.10), (2.15), (2.19), (2.22), (2.24), (2.27) to (2.32), and (3.1) to (3.6) represent a system of 17 equations in the 17 unknowns $\pi_0(0)$, ι , $r_{e,0}$, γ_y , γ_s , T , $V(k_{s,0}(0))$, $V_{k_s}(k_{s,0}(0))$, $\pi_{k_s,0}(0)$, $k_{s,0}(0)$, w_0 , α_e , α_s , $\mu(0)$, γ_v , γ_z and ρ . The results will now be reported.

3.3. Findings

Values of 0.11 and 0.16 are found for α_e and α_s , respectively. This implies that $\alpha_e + \alpha_s + \beta = 0.95$, so pure rents (before maintenance costs) are about 5% of income. The rate of time preference, ρ , has a value of 0.092. This yields an interest rate of 10%, a number somewhat larger than that of 6.9% calculated by Cooley and Prescott (1995) for the 1954-1992 period.¹⁰ Cooley and Prescott's

¹⁰Surprisingly, 10% is same real interest rate that Taubman and Rasche (1969) used in their study of office buildings.

(1995) number is probably too low for the purposes here, though, since they included the value of land in the definition of the physical capital stock which works to reduce their estimated return on capital.

The rate of technological progress in structures is found to be 1.77% a year; that, is $\gamma_v = 0.0177$. Consequently, a forgone unit of consumption can purchase 1.77% more efficiency units of structures each year. This is smaller than the 3.2% estimated for equipment, but casual empiricism suggests that technological progress has been much less in the building sector. The rate of neutral technological progress is 0.24%, or $\gamma_z = 0.0024$.

The contribution of each source of technological progress to economic growth can be calculated using (2.22) as follows:

$$f_q = \frac{\alpha_e/[1 - \alpha_e - \alpha_s]\gamma_q}{\gamma_y} = 0.41,$$

$$f_v = \frac{\alpha_s/[1 - \alpha_e - \alpha_s]\gamma_v}{\gamma_y} = 0.32,$$

and

$$f_z = \frac{1/[1 - \alpha_e - \alpha_s]\gamma_z}{\gamma_y} = 0.27,$$

where f_q , f_v , and f_z denote the fractions of output growth that is accounted for by equipment-specific, structure-specific and neutral technological progress. As can be seen, structure-specific technological progress accounts for 32%. Overall investment-specific technological progress, or technological progress in the capital goods sectors, generates nearly three-quarters of overall growth.

3.3.1. Capital Stock and Depreciation Measures

The numbers in the NIPA imply that the real stock of structures per manhour worked grew at an annual rate of 0.75% over the 1959-1996 period. The current

analysis suggests, on the basis of equation (2.21), that it grew at 3.0% over this period. Likewise, the NIPA figures indicate that the annual growth rate in the stock of equipment per manhour worked was 2.5%. The estimate obtained from (2.20) is 4.42%. The failure to incorporate technological progress in the production of new capital goods, or neglecting the terms q , γ_q , v and γ_v in (2.5), (2.20), (2.4), and (2.21), has significant consequences for the measurement of the effective capital stock.

The numbers in the NIPA do not measure physical depreciation, as is conventionally assumed in macroeconomics. The NIPA measures are based on straight-line depreciation over the *economic* service life of an asset (and not its physical service life). Hotelling (1925) introduced the concept of economic depreciation, defining it to be the rate of decline in the value of the asset over time. Let $\Pi_0(j)$ be the date-0 present value of rents (net of maintenance costs) for an age- j building until the next replacement date $T - j$.¹¹ Now, imagine constructing an annual measure of depreciation. The annual rate of economic depreciation that transpires between year 0 and year -1 is simply given by $[\Pi_0(j) - \Pi_{-1}(j - 1)]/\Pi_{-1}(j - 1)$. The rate of straight-line depreciation would be $(1/T)/[1 - (j - 1)/T]$; note the importance of the replacement date, T , in this formula. Table 4 gives these depreciation rates for selected ages of a building. Observe how the rate of depreciation grows slowly at first and then accelerates rapidly toward the end of the building's life.¹² Note that the average rates of depreciation are somewhat higher than the

¹¹That is, $\Pi_0(j) = \int_0^{T-j} [\pi_t(j+t) - \mu(j+t)k_{s,-j}(0)/v_{-j}]e^{-\iota t} dt$. Assume that at the time of construction the owner purchases the structure and obtains a lease to the land for T years. The date-0 cost and benefit of doing this would be $\Pi_0(0)$.

¹²The rate of economic depreciation is very low early on. Taubman and Rasche (1969) constructed a similar table to argue that tax laws allowed depreciation allowances that were too

5.6% used for structures in the NIPA.¹³

Table 4		
Age (years)	Econ. Dep., %	St. Line Dep., %
1	2.56	1.92
5	2.62	2.08
15	2.83	2.63
30	3.78	4.35
40	6.40	7.69
50	31.70	33.3
51	48.72	50.00
52	100.00	100.00
Econ. Dep. — mean: 8.28%		
St. Line Dep. — mean: 8.73%		

3.3.2. Statistical Robustness

The analysis hinges on the estimated value for the rent gradient. How sensitive are the results to this parameter? To answer this question note that the model defines two mappings Γ_v and F_v such that $\gamma_v = \Gamma_v(\delta_s)$ and $f_v = F_v(\delta_s)$; that is, the model returns values for the rate of structure-specific technological progress and its contribution to economic growth, given an estimate for the rent gradient. It turns out that (numerically) these mappings are monotonically decreasing in δ_s . In other words, the steeper the rent gradient is (or the smaller is δ_s), the faster is the pace of structure-specific technological progress and the larger is its contribution

generous, because of this fact.

¹³Once again, as calculated by Greenwood, Hercowitz and Krusell (1997).

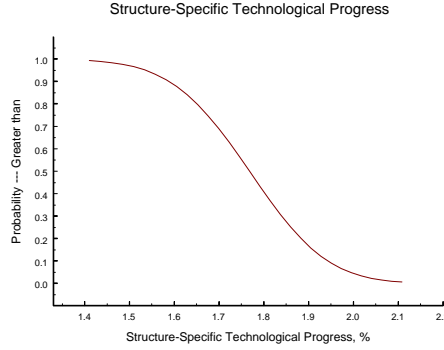


Figure 3.3:

to growth. Therefore, $\Pr[\gamma_v \geq x] = \Pr[\delta_s \leq \Gamma_v^{-1}(x)]$ and $\Pr[f_v \geq x] = \Pr[\delta_s \leq F_v^{-1}(x)]$. Now, the estimate of the rent gradient is a normally distributed random variable with mean 0.023 and standard deviation 0.002. Given this, what do the distributions for $\Pr[\gamma_v \geq x]$ and $\Pr[f_v \geq x]$ look like?

Figures 3.3 and 3.4 plot the distributions for $\Pr[\gamma_v \geq x]$ and $\Pr[f_v \geq x]$. As can be seen from Figure 3.3, the probability that structure-specific technological progress is greater than 1.4% is almost certain. But it is almost certainly true too that it is less than equipment-specific technological progress. Likewise, Figure 3.4 shows the odds that structure-specific progress accounts for at least 20% of growth are excellent; yet, that it contributes more than 40% to growth looks remote.

4. Conclusion

The analysis here takes a different route to measuring technological progress than the one typically travelled by growth accountants. Price data is used to shed

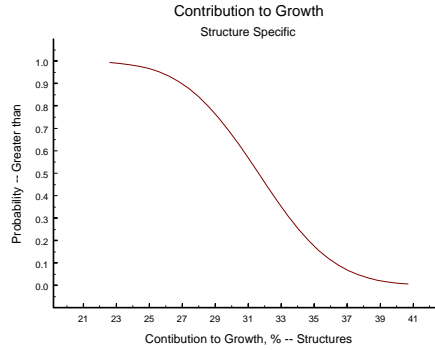


Figure 3.4:

information on the sources of economic growth. Over the postwar period, the relative price of equipment has fallen dramatically. This suggests that there is technological change in the equipment-producing sector of the economy. Similarly, rents decline with the age of a building, holding fixed factors such as repair and maintenance. Perhaps this is because new buildings embody new and improved technology in their structures. By casting the analysis in a general equilibrium setting, a link can be established between the observed rent gradient and the rate of technological progress in buildings. Likewise, the tie between the decline in the relative price of equipment and equipment-specific technological progress is made explicit. Similarly, the connection can be derived between, on the one hand, the observed data on the average age of structures, the structures investment-to-GDP ratio and the equipment investment-to-GDP ratio, and on the other one hand, the implied shares of structures and equipment in GDP and the interest rate.

The upshot of the analysis is that the rate of structure-specific technological progress is about 1.77% a year. This implies that 32% of economic growth can

be attributed to structure-specific technological progress. Given that it is also found that equipment-specific technological progress accounts for 41% of growth, the conclusion is that 73% of economic growth is due to technological progress embodied in the form of new capital goods.

References

- [1] Cooley, Thomas F. and Edward C. Prescott, “Economic Growth and Business Cycles”, in Thomas F. Cooley (ed.) *Frontiers of Business Cycle Theory*, Princeton University Press, Princeton, N.J., 1995: 1-38.
- [2] Gordon, Robert J. *The Measurement of Durable Goods Prices*, University of Chicago Press, Chicago, 1990.
- [3] Greenwood, Jeremy; Hercowitz, Zvi; and Per Krusell, “The Macroeconomic Implications of Investment-Specific Technological Change,” *American Economic Review* 87, no. 3 (June 1997): 342-362.
- [4] Hotelling, Harold, “A General Mathematical Theory of Depreciation,” *Journal of the American Statistical Association* 20, no. 153 (September 1925): 340-353.
- [5] Taubman, Paul and Robert H. Rasche, “Economic and Tax Depreciation of Office Buildings,” *National Tax Journal* XXII, no. 3 (September 1969): 334-346.