# Nonlinearities in the Regional Phillips Curve with Labor Market Tightness

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- The Phillips curve formalizes an intuitive idea
  - In tight labor markets, marginal costs increase and pass through price inflation
  - Aggregate supply curve of New Keynesian models
  - The slope of the Phillips curve is the elasticity of that supply curve
- Phillips curve estimation is challenging

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  - Potentially state-dependent parameters

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  - The slope of the Phillips curve is the elasticity of that supply curve
- Phillips curve estimation is challenging
  - Main empirical challenges
- Emergent literature argues for the usefulness of cross-sectional Phillips curves

$$\pi_{jt} = \mathbf{\gamma}_t - \mathbf{\psi}(u_{jt} - u_{jt}^*) + \vartheta_{jt}$$

## Gitti (2024)

Main object of interest: Non-linear regional Phillips curve (NRPC)

- Two main contributions
  - Argue that  $\log\left(\frac{v}{u}\right)$  is a better measure of slack than  $u \to$  Theory
  - Estimate changes in the slope of the NRPC in the cross-section pre vs. post Covid → Empirical
- Importance of the contribution
  - Most theories on the change of the slope of the Phillips curve are external to it
    - Examples: Globalization, market power
  - Here cyclical demand will generate changes in the supply elasticity
  - ... and map very cleanly to an estimating equation
  - Informative on the debate of the supply vs. demand shifters behind inflation surge of 2021

#### **Discussion Roadmap**

- Evaluation: Important, well-executed paper, in an exciting research agenda
- I will focus on two comments
  - Identification of the parameters of interest
  - Thoughts on orders of magnitude

NRPC

• Simplified framework: Many terms collapsed into ε<sub>it</sub>

$$\pi_{it} = \beta \mathbb{E}_t \pi_{i,t+1} + \kappa_{it} \hat{\theta}_{it} + \varepsilon_{it}$$

$$\kappa_{it} = \begin{cases} \kappa & \text{if } \hat{\theta}_{it} \leq \hat{\theta}^* \\ \kappa(1+\lambda) & \text{otherwise.} \end{cases}$$

- Pedagogic assumptions:
  - $\hat{\theta}$  follows an AR(1) with coef.  $\rho$
  - Same  $\rho$  regardless of slack vs. tight labor market
  - Perfect foresight. Only one shock in each region in period t

(1)

(2)

## Two regions

• Two regions. Small and Large shocks

$$\pi_{it} = \frac{\kappa}{1 - \beta \rho} \hat{\theta}_{S}$$
(3)  
$$\pi_{jt} = \frac{\kappa}{1 - \beta \rho} \left( 1 + \lambda \left( 1 - (\beta \rho)^{\tilde{T}} \right) \right) \hat{\theta}_{L}$$
(4)

- $\tilde{T}$  endogenous. Furthermost period with tight labor market given an initial shock  $\hat{\theta}_L$
- Differential inflationary effect of a tight economy:

$$\frac{\partial \pi_{jt}}{\partial \theta_L} - \frac{\partial \pi_{it}}{\partial \theta_S} = \lambda \kappa \frac{1 - (\beta \rho)^{\tilde{T}}}{1 - \beta \rho}$$
(5)

### Identification

$$\frac{\partial \pi_{jt}}{\partial \theta_L} - \frac{\partial \pi_{it}}{\partial \theta_S} = \lambda \kappa \frac{1 - (\beta \rho)^{\tilde{T}}}{1 - \beta \rho}$$

- Empirical object is the LHS. Coefficient of interest is  $\boldsymbol{\lambda}$
- Uninteracted estimates in the paper suggest  $\kappa/(1-\beta\rho)$  is small
- If  $\tilde{T} \approx 1$ , then  $\left(1 (\beta \rho)^{\tilde{T}}\right) \approx 0$
- If  $\tilde{T} \to \infty$ , then  $\left(1 (\beta \rho)^{\tilde{T}}\right) \approx 1$
- *T* is a nuisance parameter. Need to take a stance on it before using the empirical moment to infer about λ.

(6)

### Identification

- Issue is compounded if we relax equal dynamics of  $\theta$  in slack and tight markets
- Now assume:
  - In slack markets: AR(1) with coef.  $\rho$
  - In tight markets: AR(1) with coef:  $\omega$
- In reality the dynamics of  $\theta$  may be far from an AR(1)

### Identification

$$\frac{\partial \pi_{jt}}{\partial \theta_L} - \frac{\partial \pi_{jt}}{\partial \theta_S} = \lambda \kappa \frac{1 - (\beta \omega)^{\tilde{T}}}{1 - \beta \rho} + \kappa \beta \frac{\omega - \rho}{(1 - \beta \omega)(1 - \beta \rho)}$$

- First term very similar than before, but now a function of  $\boldsymbol{\omega}$
- New term that needs to be cleaned. Sign and magnitudes are unclear
- Empirical moment may be large even if  $\lambda = 0$
- ...or may introduce downward bias in  $\lambda$

My suggestion: Test the AR(1) with equal parameter assumption in the data. If dynamics are richer, embrace them.

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$$\pi_{t-12,t} = 2\% + 0.16 \log(\theta_t) + 1.79 \log(\theta_t) \mathbb{1}_{\theta_t > 1} - 0.15 \mathbb{1}_{\theta_t > 1}$$



- At face value the estimates can explain  $\approx 30\%$  of the inflation surge
- The paper could do more to address implicit assumptions of this figure
  - I am plugging the cross-sectional estimates in the aggregate data
    - The persistence of local  $\theta$  may be very different than the persistence of national  $\theta$
    - My figure assumes they are the same
    - We know the volatility is very different
  - I am also assuming  $\kappa$  and  $\lambda$  at the regional level map directly into the aggregate