

Nonlinear Bank Capital Regulation

Maximilian Jager and Karl Schulz

**Cleveland Fed Financial Stability Conference
2025**

Discussion by Pab Jotikasthira
SMU - Dallas

Summary

Presents **a unifying framework for bank capital regulation**, and uses the perturbation approach with a few calibrated sufficient statistics to perform “quantitative” positive and normative analyses (e.g., assessing different policy proposals).

Entrepreneurs: $\mathcal{V}_\theta^E = \max_{d_\theta} U_\theta^E(d_\theta; k_\theta, z_\theta) \quad \text{s.t.} \quad \mathcal{C}_\theta^E(d_\theta; k_\theta, z_\theta) \leq 0,$

Households (depositors): $\mathcal{V}^H = \max_c U^H(c; x) \quad \text{s.t.} \quad \mathcal{C}^H(c; x) \leq 0.$

Bank:

$\mathcal{V}^B = \max_{x,p} U^B(x, p) \quad \text{s.t.} \quad \mathcal{P}(p_\theta, k_\theta, z_\theta; d_\theta, \theta) = 0, \forall \theta, \quad \mathcal{C}(x, p; c, d) \leq 0, \quad \mathcal{R}(x, p) \leq 0.$

where $\mathcal{R}(k, \mathcal{E}, p) \equiv \int_{\Theta} \omega(p_\theta) k_\theta d\theta - \mathcal{E}/\Omega \leq 0.$

Nonlinear capital regulation
(nonlinear function of default risk)

Capital adequacy ratio,
e.g., 8%

Summary –cont'd

In equilibrium (all agents respond optimally to others), behavioral responses can be characterized by the following sufficient statistics:

$$\zeta_{\theta}^{k,\omega} \equiv \left. \frac{\partial \log k_{\theta}}{\partial \omega(p_{\theta})} \right|_p, \quad \zeta_{\theta}^{k,\omega'} \equiv \left. \frac{\partial \log k_{\theta}}{\partial \omega'(p_{\theta})} \right|_p, \quad \zeta_{\theta}^{k,p} \equiv \frac{\partial \log k_{\theta}}{\partial \log \bar{p}_{\theta}}, \quad \varepsilon_{\theta}^{p,k} \equiv \frac{d \log p_{\theta}}{d \log k_{\theta}}.$$

Also needs a few marginal welfare externalities to be able to perform normative analyses:

$$\chi^H \equiv -\frac{1}{\mu} \frac{d\mathcal{V}^H}{d\mathcal{E}} \quad \xi_{\theta}^H \equiv -\frac{1}{\mu} \frac{d\mathcal{V}^H}{dk_{\theta}} \quad \text{and} \quad \xi_{\theta}^E \equiv -\frac{1}{\mu} \frac{d\mathcal{V}_{\theta}^E}{dk_{\theta}}, \quad \forall \theta.$$

These statistics are then estimated using detailed German credit registry data (where banks provide probability of default estimate for each loan).

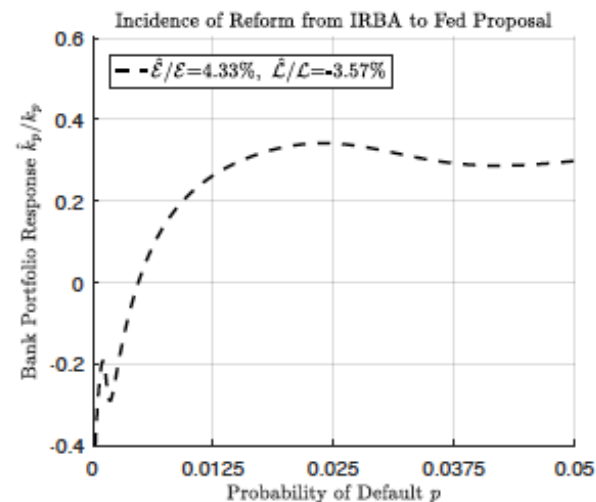
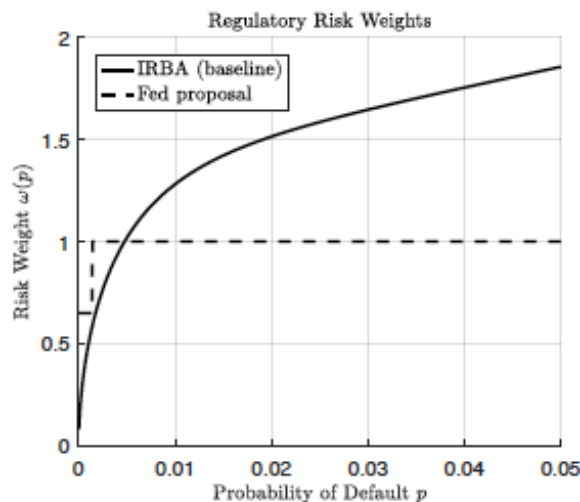
	Homogeneous (1)	Risk Category 1 (2)	Risk Category 2 (3)	Risk Category 3 (4)	Risk Category 4 (5)
$\log(\widehat{credit}_{i,t-1})$	0.019*** (0.002)	0.019*** (0.004)	0.011*** (0.002)	0.023*** (0.002)	-0.024*** (0.004)
Firm FE	Y	Y	Y	Y	Y
Time FE	Y	Y	Y	Y	Y
Obs.	280,171	7,334	30,392	213,491	26,528
R^2	0.693	0.733	0.536	0.632	0.635

Table 4: Estimated credit-risk elasticities (German credit registry).

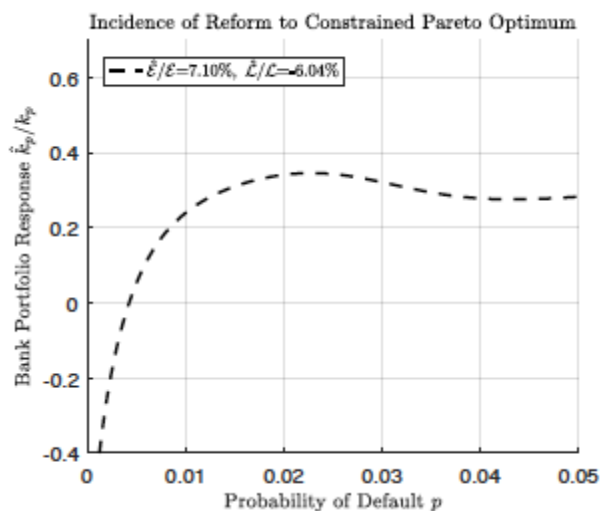
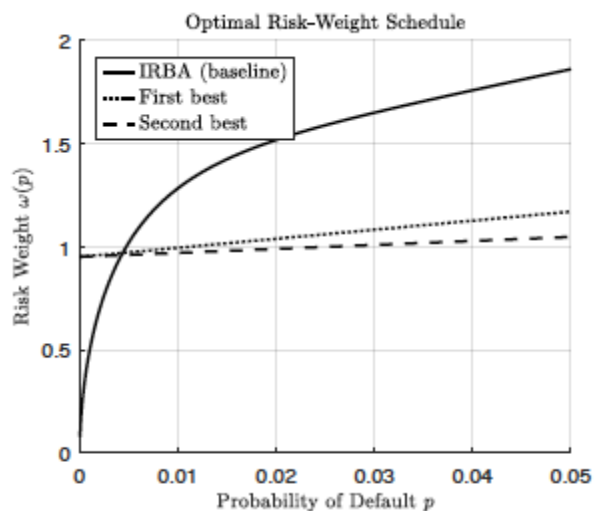
	Homogeneous (1)	Risk Category 1 (2)	Risk Category 2 (3)	Risk Category 3 (4)	Risk Category 4 (5)
$\log(p_{i,b,t-1})$	-0.063*** (0.017)	-0.006 (0.091)	0.045 (0.050)	-0.049** (0.018)	-0.129*** (0.027)
$\omega_{i,b,t-1}$	-0.759*** (0.124)	-1.289*** (0.370)	-1.430*** (0.280)	-0.732*** (0.121)	-0.271*** (0.052)
Bank FE	Y	Y	Y	Y	Y
Borrower x Time FE	Y	Y	Y	Y	Y
Obs.	1,616,772	82,962	213,888	909,427	62,196
R^2	0.677	0.605	0.646	0.692	0.719

Table 5: Estimated credit-supply elasticities (German credit registry).

We can then assess policy – e.g., the Fed’s Basel Endgame



And, we can obtain “optimal” risk weights:



My Thoughts

Ambitious paper addressing important question!

- Circumventing complex theory and specific designs using sufficient statistics.
- Flexible and easy to calibrate, permitting positive and normative analyses around the observed equilibrium.

Generality comes at a cost ...

- Silent on exact economic mechanisms and decisions (price, in particular, is missing).
- Needs assumptions anyway when calibrate.
- Results are local and may not be generalized for complex, nonlinear models.

1. Economic Mechanisms

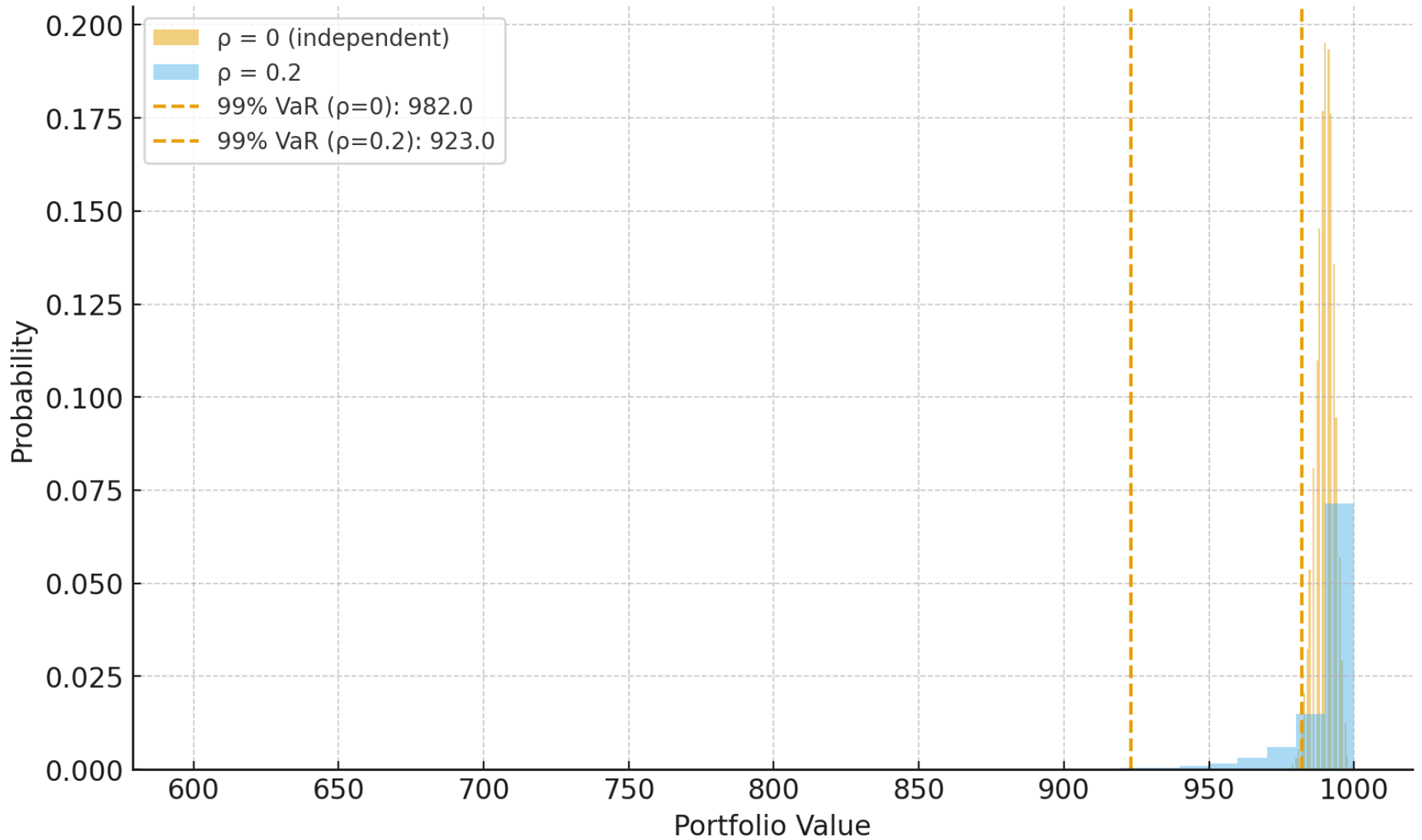
- Silent.
 - Signs of sufficient statistic estimates may be consistent with some mechanisms but not others.
 - No system to look across all estimates to pin down the exact model.
 - Not transparent on missing ingredients and simplifying assumptions.
- **Cross-loan spillovers and correlations?**
 - Only see substitution but it's not the same.
 - Not clear why the MRS are not part of sufficient statistics and not estimated

$$\frac{\hat{k}_\theta}{k_\theta} = \zeta_\theta^{k,\omega} \hat{\omega}(p_\theta) + \zeta_\theta^{k,\omega'} \hat{\omega}'(p_\theta) + \varepsilon_\theta^{k,p} \frac{\hat{p}_\theta}{p_\theta} - \frac{\partial MRS_\theta}{\partial \mathcal{E}} \frac{\hat{\mathcal{E}}}{k_\theta} - \int_{\theta'} \left(\frac{\partial MRS_\theta}{\partial k_{\theta'}} \frac{\hat{k}_{\theta'}}{k_\theta} + \frac{\partial MRS_\theta}{\partial \bar{p}_{\theta'}} \frac{\hat{p}_{\theta'}}{k_\theta} \right) d\theta'.$$

1. Economic Mechanisms –cont'd

- **Risk pricing** and capital adequacy must be used together.
 - The authors wonder why the sensitivity of credit to risk is weak, and mention price adjustments as perhaps a reason.
 - Without frictions, **price NOT quantity captures the expected default loss** (plus risk premium, etc.)
 - **Capital captures the “unexpected” loss (or, $\text{VaR} - \text{EL}$)**. Default probability is actually not a sufficient statistic for unexpected losses.
 - Price is part of many canonical models, and is also observable.

Normalized Portfolio Value Distribution with 99% VaR



2. Calibration Problems

- Adhoc assumptions are made in the calibration, diminishing generality.
- For example, profits = utility. Where is risk? Firms maximize one-period profits?
- Externalities on households are just the losses in bailout?

of the bank $\Pi^B(\cdot, v)$. Letting $\kappa_{\mathcal{T}} = 25\%$ denote the deadweight cost of deposit insurance, the total fiscal externality is

$$-(1 + \kappa_{\mathcal{T}})\mathcal{T}, \quad \text{where} \quad \mathcal{T} \equiv \max\{0, \mathcal{D} - \Pi^B(\cdot, v)\}.$$

The state-contingent going concern value of the bank consists of total loan repayments (loan rate $r = 4.68\%$; see Corbae and D'Erasmus (2021)), recovered loans in default (recovery rate $\phi = 0.6030$; see Corbae and D'Erasmus (2021)), and the post-liquidation value of the loan portfolio (depreciation rate $\iota = 0.1965$; see Corbae and D'Erasmus (2021)):

$$\Pi^B(\cdot, v) = \int_{\Theta} [v(1 + r)(1 - p_{\theta}) + (1 - \phi)p_{\theta} - \iota] k_{\theta} d\theta.$$

- Even the proper estimation of sensitivities is not coherent.

2. Calibration Problems –cont'd

$$\log(\text{credit}_{i,b,t}) = \gamma(\text{BankLevy}_{b,t-1} \times \text{LevyIntroduction}_t) + p_{i,b,t-1} + \beta X_{b,t-1} + \mu_{i,t} + \mu_b + v_{i,t}$$

and

$$p_{i,t} = \zeta_p^{p,k} \log(\widehat{\text{credit}}_{i,t-1}) + \beta X_{i,t-1} + \mu_i + \mu_t + u_{i,t}$$

Should have bank-firm fixed effects (b,i)

Should include all controls from above especially past default probability

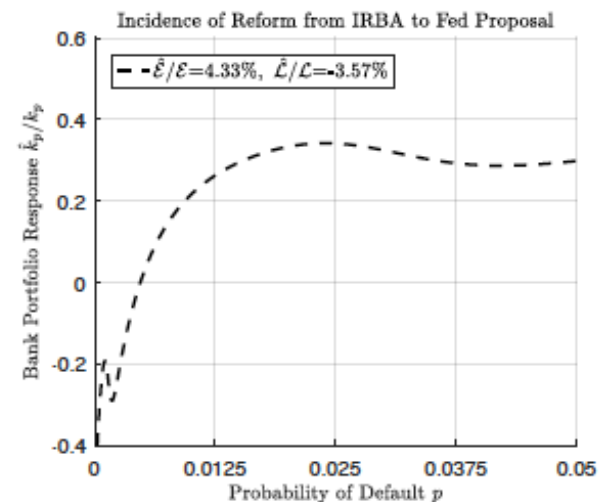
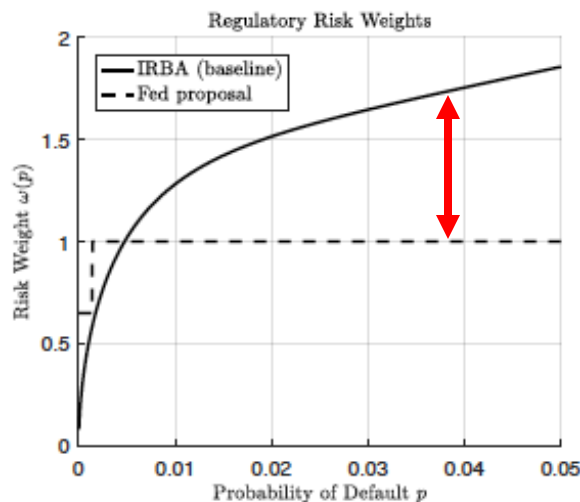
Why not the same equation?

$$\log(\text{credit}_{b,i,t}) = \varepsilon_p^{k,p} \log(p_{i,b,t-1}) + \zeta_p^{k,w} \omega_{i,b,t-1} + X_{b,t-1} + \mu_b + \mu_{i,t} + u_{i,t}$$

Where is the slope effect (w')? How to proxy for it?

3. Local vs. Global Assessment

- Sensitivity estimates are local, but some of the assessments look at large changes.



	Homogeneous (1)	Risk Category 1 (2)	Risk Category 2 (3)	Risk Category 3 (4)	Risk Category 4 (5)
$\log(p_{i,b,t-1})$	-0.063*** (0.017)	-0.006 (0.091)	0.045 (0.050)	-0.049** (0.018)	-0.129*** (0.027)
$\omega_{i,b,t-1}$	-0.759*** (0.124)	-1.289*** (0.370)	-1.430*** (0.280)	-0.732*** (0.121)	-0.271*** (0.052)

To Conclude ...

Ambitious paper addressing important question!

- Circumventing complex theory and specific designs using sufficient statistics from a general model.
- Interesting policy-relevant results.

My two cents ...

- Bring in price and cross-loan correlations. Discuss the sufficient statistic estimates, taken together – consistent with which models?
- Motivate assumptions used in the calibration, and perform sensitivity analysis. Can we really take the quantitative exercise seriously? Any standard error bound?
- Be careful extrapolating beyond the local estimates.