

Heterogeneous Price Rigidities and Monetary Policy

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May 16, 2019

Introduction

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 - ▶ Incidence of unemployment
 - ▶ Income composition
 - ▶ Cash holdings heterogeneity

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 - ▶ Normative perspective
 - ▶ But also positive implications for MP transmission mechanism
- Previous work:
 - ▶ Savers and debtors
 - ▶ Incidence of unemployment
 - ▶ Income composition
 - ▶ Cash holdings heterogeneity
- Does heterogeneity in price rigidities across sectors matter?
 - ▶ Price stickiness is source of monetary non-neutrality in NK models
 - ▶ Price stickiness is known to be heterogeneous across sectors
 - ▶ What are the implications for distributional and/or aggregate effects of MP?

This paper

1. New stylized facts (BLS/CEX/ACS data): prices are more rigid in industries...
 - ▶ ... selling to richer/more educated households (“expenditure channel”)
 - ▶ ... employing richer/more education households (“earnings channel”)
 - ▶ Example: services and manufacturing

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 - ▶ Example: services and manufacturing
2. Heterogeneous Agent New Keynesian model with many sectors and household types
 - ▶ Quantify the aggregate and distributional implications
 - ▶ Consumption of college-educated households is 30% more sensitive
 - ▶ Aggregate real effect of a 100bps MP tightening is dampened by 7%

Literature

Distributional implications of MP: Doepke and Schneider (2006), Carpenter and Rogers (2004), Albanesi (2007), Williamson (2009), Ledoit (2009), Coibion et al. (2016), Auclert (2017)

Empirical work on price stickiness: Blinder et al. (2008), Bils and Klenow (2002, 2004), Bils et al. (2003), Klenow and Kryvtsov (2008), Nakamura and Steinsson (2008)

Models with heterogeneous price stickiness: Aoki (2001), Bils and Klenow (2002), Carlstrom et al. (2006), Carvalho (2006), Barsky et al. (2006), Nakamura and Steinsson (2007)

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Our contribution: We study an enriched HANK model with firm and household heterogeneity.

Outline

1. Conceptual framework
2. Data and stylized facts
3. Quantitative analysis

The simple model

- Two periods: $t = 1, 2$
- Two sectors: $s \in \{A, B\}$
- Finite household types i with different sectoral exposures

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Household i solves:

$$\max \sum_{t=1}^2 \beta^{t-1} U[(c_{i,t}^A)^{1-\alpha^i} (c_{i,t}^B)^{\alpha^i}]$$

subject to

$$\underbrace{c_{i,1}^A + \frac{c_{i,2}^A}{R}}_{\text{Spending on A}} + \underbrace{p_1 c_{i,1}^B + p_2 \frac{c_{i,2}^B}{R}}_{\text{Spending on B}} = \underbrace{\frac{b_{i,1}}{\pi_1^A}}_{\text{Initial wealth}} + \underbrace{\gamma^i (Y_1^A) + \frac{\gamma^i (Y_2^A)}{R}}_{\text{Earnings from A}} + \underbrace{p_1 \gamma^i (Y_1^B) + p_2 \frac{\gamma^i (Y_2^B)}{R}}_{\text{Earnings from B}}$$

where $p_t = \frac{P_t^B}{P_t^A}$ is **relative price**, α^i **expenditure exposure** and γ^i **earnings exposure**.

Simple perturbation: partial equilibrium

- Consider the general perturbation $\{dR, dY_1^A, dY_1^B, dp, d\pi^A\}$

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$$MPC_{i,1} \equiv \frac{\partial}{\partial y_i} p^{\alpha^i} c_{i,1}.$$

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Proposition: Household i 's behavioral consumption response can be decomposed into

$$dc_{i,1} = \underbrace{-\frac{1}{\gamma} MPS_{i,1} c_{i,1} \frac{dR}{R}}_{\text{Substitution effect}} + MPC_{i,1} \left\{ \underbrace{\left\{ b_{i,2} \frac{dR}{R} \right\}}_{\text{Interest rate exposure}} - \underbrace{\left\{ \frac{b_{i,1}}{\pi^A} \frac{dP^A}{P^A} \right\}}_{\text{Bond revaluation}} \right. \\ \left. + \underbrace{\gamma_i^A dY_1^A + p \gamma_i^B dY_1^B}_{\text{Heterogeneous earnings channel}} + \underbrace{\gamma_i^B p \left(Y_1^B + \frac{1}{R} Y_2^B \right) \frac{dp}{p}}_{\text{Relative price effect on real earnings}} - \underbrace{\alpha^i p^{\alpha^i} \left(c_{i,1} + \frac{1}{R} c_{i,2} \right) \frac{dp}{p}}_{\text{Relative price effect on real expenditures}} \right\}.$$

Simple perturbation: general equilibrium

Proposition: In response to our proposed aggregate perturbation, the change in aggregate demand can be decomposed as

$$\begin{aligned}
 dY_1 = & \left[\text{Cov}_I \left(\mu \text{MPC}_{i,1}, b_{i,2} \right) - \frac{1}{\gamma} \mathbb{E}_I (\mu \text{MPS}_{i,1} c_{i,1}) \right] \frac{dR}{R} - \text{Cov}_I \left(\mu \text{MPC}_{i,1}, \frac{b_{i,1}}{\pi^A} \right) \frac{dP^A}{P^A} \\
 & + \underbrace{\sum_s \frac{P_t^s}{P_t^A} \left(\mathbb{E}_I (\text{MPC}_{i,1}) + \text{Cov}_I (\mu \text{MPC}_{i,1}, \gamma_i^s) \right) dY_1^s}_{\text{Heterogeneous earnings effect}} \\
 & + \sum_t \frac{1}{R^{t-1}} \underbrace{p \left(\mathbb{E}_I (\text{MPC}_{i,1}) + \text{Cov}_I (\mu \text{MPC}_{i,1}, \gamma_i^B) \right) Y_t^B \frac{dp}{p}}_{\text{Relative price effect on earnings}} \\
 & - \sum_t \frac{1}{R^{t-1}} \underbrace{\mathbb{E}_I \left(\mu \text{MPC}_{i,1} \alpha^i p^{\alpha^i} c_{i,t} \right) \frac{dp}{p}}_{\text{Relative price effect on expenditures}} .
 \end{aligned}$$

Outline

1. Conceptual framework
2. Data and stylized facts
3. Quantitative analysis

Data

- Build 3 linked datasets with price rigidities (consumer and producer prices), expenditures and payrolls
 - ▶ Covers full U.S. economy (except shelter in most cases)
- CPI-ACS sample:
 - ▶ merge price rigidity data from Nakamura and Steinsson (2008) (at the ELI level) to earnings data from the ACS (at the industry level)
- PPI-ACS sample:
 - ▶ match price rigidity data from Pasten et al. (2016) (at the 6-digit NAICS level) to ACS industries
- CPI-CEX sample:
 - ▶ merge price rigidity data from Nakamura and Steinsson (2008) (at the ELI level) to spending data from the CEX (at the UCC level).

New facts

Two empirical findings:

1. Prices more rigid in product categories selling to more educated/richer households (consistent with Cravino-Lan-Levchenko, 2019)

Examples:

- ▶ Services (frequency: 6.39%, share of sales to College: 37.9%)
- ▶ Taxi fares (frequency: 4.41%, share of sales to College: 62.3%)
- ▶ Fast food lunch (frequency: 7%, share of sales to College: 34.4%)

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Examples:

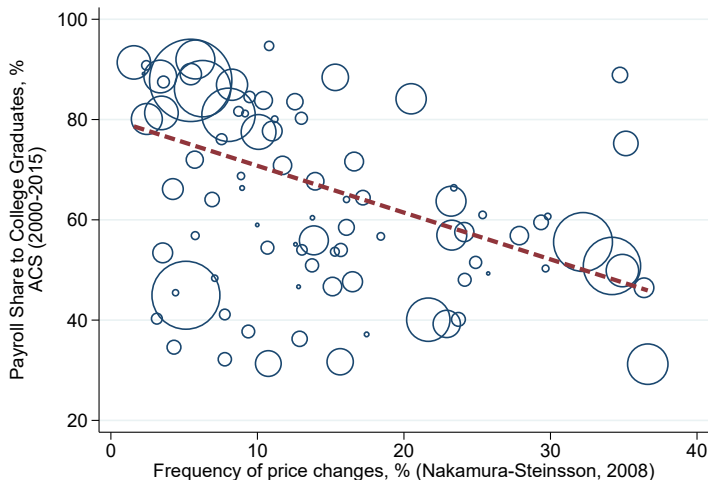
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2. Prices more rigid in product categories employing more educated/richer households

Examples:

- ▶ Computer electronics (frequency: 28.95%, payroll share to College: 72.15%)
- ▶ Poultry processing (frequency: 35.1%, payroll share to College: 14.43%)

Earnings channel: CPI-ACS

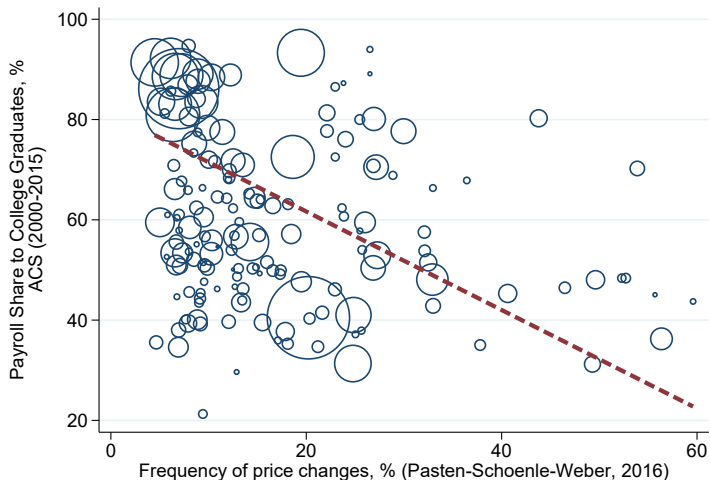


Notes: Includes All Prices Changes

Earnings channel: CPI-ACS

	Share of Payroll to College Graduates (%)		
	(1)	(2)	(3)
Frequency of Price Changes (%)	-0.9330*** (0.2649)	-0.463** (0.2119)	-0.5505** (0.2396)
Excluding industries with price change frequency > p95	Yes	Yes	No
2-digit Naics Code F.E.	No	Yes	No
Sample Size	86	86	94

Earnings channel: PPI-ACS

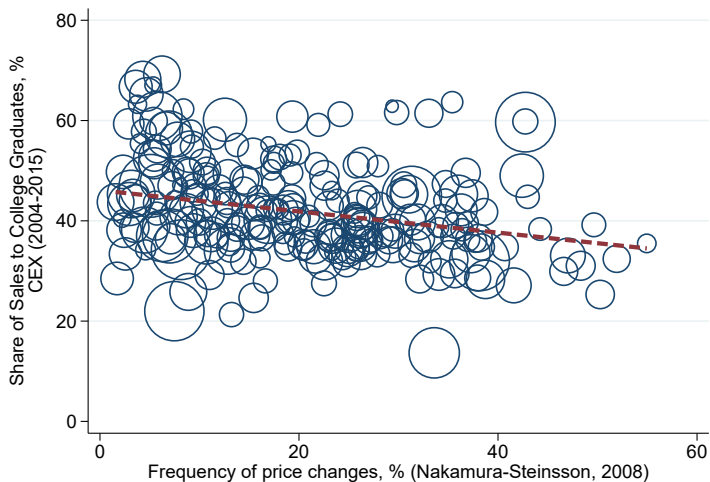


Notes: Includes All Prices Changes

Earnings channel: PPI-ACS

	Share of Payroll to College Graduates (%)		
	(1)	(2)	(3)
Frequency of Price Changes (%)	-0.9823*** (0.2149)	-0.2027 (0.1306)	-0.3771* (0.1978)
Excluding industries with price change frequency > p95	Yes	Yes	No
2-digit Naics Code F.E.	No	Yes	No
Sample Size	163	163	169

Expenditure channel: CPI-CEX

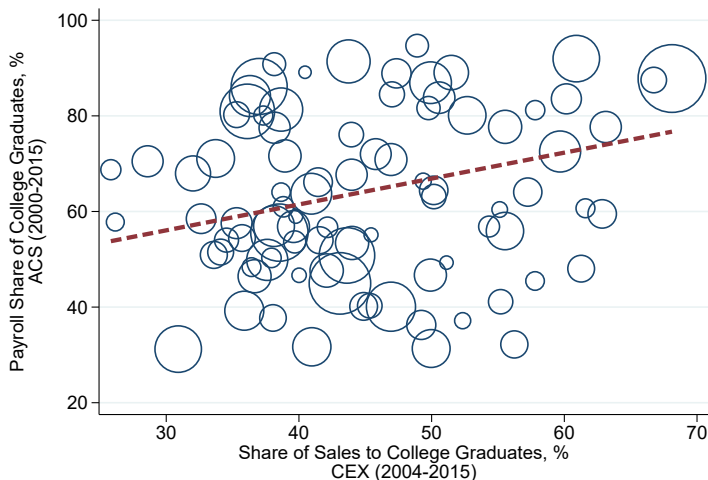


Notes: Includes All Prices Changes

Expenditure channel: CPI-CEX

	Share of Sales to College Graduates (%)		
	(1)	(2)	(3)
Frequency of Price Changes (%)	-0.2108** (0.0824)	-0.1904* (0.0977)	-0.1256** (0.0376)
Excluding industries with price change frequency > p95	Yes	Yes	No
Expenditure Category F.E.	No	Yes	No
Sample Size	242	242	254

Interaction between Earnings / Expenditure channels



Notes: OLS Coeff. 0.5416*** (s.e. 0.2264), N=88

New facts

- Implications for monetary policy tightening:
 - ▶ NK model prediction for sector with more rigid prices: less deflation, but bigger output gap
 - ▶ More educated households suffer more: preferred goods relatively more expensive, stronger labor demand contraction
 - ▶ Feedback loop on consumption of more educated households: demand for goods in more rigid sector falls even more (→ relative price, labor demand)
 - ▶ Monetary policy has relatively larger effect on richer, low-MPC households → dampened aggregate effect

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- Robustness

- ▶ Excluding sales
- ▶ Different measures of income and education
- ▶ Broad sector fixed effects (e.g. within goods)

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 - ▶ Sectors employ two types of workers: $N_{C,t}^s$ and $N_{NC,t}^s$
 - ▶ Each sector has its own, fully segmented labor market (business cycle frequency)

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- Two household types $i \in \{C, NC\}$: college and non-college
 - ▶ Within type heterogeneity: uninsurable earnings risk (standard incomplete markets model)
 - ▶ Different sector-specific productivities: Z_e^s (equivalent to γ_i in simple model)
 - ▶ Different tastes: α_C^s and α_{NC}^s

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- Policy experiment: contractionary 100bps monetary policy shock

Model details

- CES consumption baskets

$$c_{i,t} = \left[\sum_s^N (\alpha_i^s)^{\frac{1}{\eta}} (c_{i,t}^s)^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- Household budget constraint (assumptions on profit rebate important)

$$\underbrace{\dot{a}_{i,t} = (i_t - \pi_t^N) a_{i,t}}_{\text{Interest income}} + \underbrace{z_{i,t} n_{i,t} w_{i,t} p_{i,t}}_{\text{Labor income}} + \underbrace{\tau_{i,t} p_{i,t}}_{\text{Transfer income}} - \underbrace{c_{i,t} p_{i,t}}_{\text{Consumption}}, \quad a_{i,t} \geq \underline{a}$$

- Intermediate goods producer production function

$$Y_t^s(j) = \left[\sum_{e \in C, NC} (Z_e^s)^{\frac{1}{\kappa}} N_{e,t}^s(j)^{\frac{\kappa-1}{\kappa}} \right]^{\frac{\kappa}{\kappa-1}}$$

- Two Phillips Curves (under Rotemberg pricing)

$$\dot{\pi}_t^s = \pi_t^s \left(i_t - \pi_t^s - \frac{\dot{Y}_t^s}{Y_t^s} \right) - \frac{\epsilon - 1}{\delta^s} \left(\frac{\epsilon}{\epsilon - 1} MC_t^s - 1 \right)$$

Calibration strategy

- Heterogeneous expenditure shares: α_i^s
- Heterogeneous sectoral skill intensities: Z_e^s
- Heterogeneous sectoral price stickiness: δ^s

Summary of quantitative exercise

- Consider two cases: baseline (homogeneous price rigidities) and full model
- Cross-sectional effect: Compute distributional effects between C and NC as

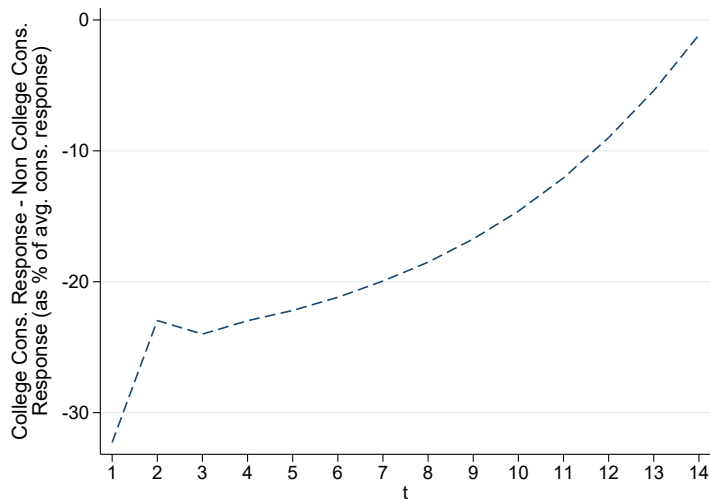
$$\Delta = \frac{\Delta C^C}{C_{SS}^C} - \frac{\Delta C^{NC}}{C_{SS}^{NC}},$$

then difference full model from baseline, $\Delta - \Delta^{baseline}$ and normalize by aggregate consumption response

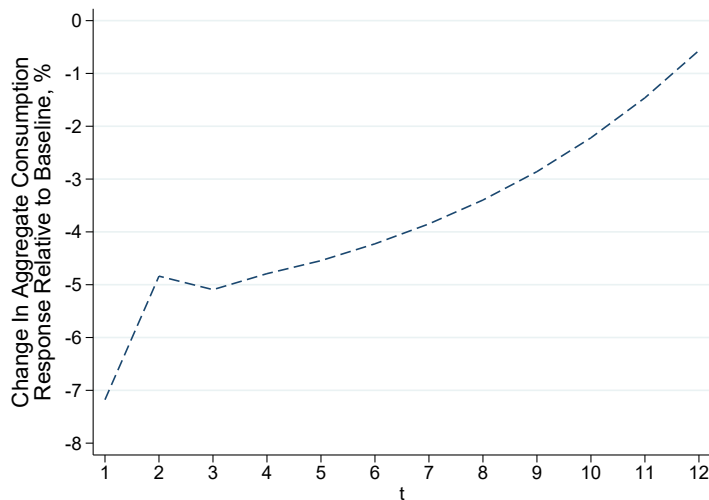
- Aggregate effect: change in aggregate consumption response in full model relative to baseline

$$\frac{\Delta C}{\Delta C^{baseline}}$$

Summary of quantitative exercise: cross-sectional



Summary of quantitative exercise: aggregate



Conclusion

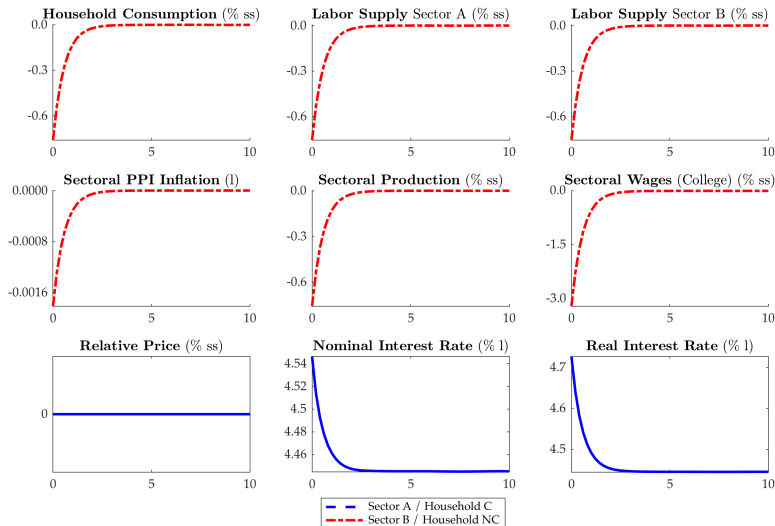
- This paper re-evaluates the implications of heterogeneous price stickiness for the transmission and the distributional effects of monetary policy
- Establish new facts using micro data:
 1. Richer/more educated households purchase in more rigid sectors
 2. Richer/more educated households work in more rigid sectors
- Quantitative model to assess implications of these new facts
 - ▶ Real effects of MP dampened in the presence of heterogeneous price stickiness
 - ▶ Consumption of college households 30% more sensitive to MP shocks
 - ▶ Aggregate effects of monetary policy muted by 5 - 10% due to novel earnings and expenditure channels

Calibration

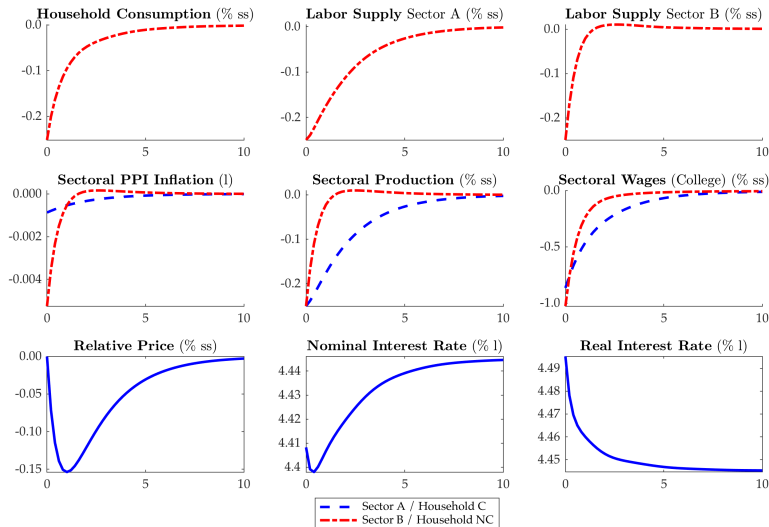
Table 1: Parameters for Calibration

		Value	Source
ϕ	Curvature of (relative) labor supply curve	1.5	Smets and Wouters (2007)
θ_C	P(Non-College College)	0.45/35	Ferrare (2016)
θ_{NC}	P(College Non-College)	0.22/35	
ϵ	Elasticity of substitution between intermediates	11	Basu and Fernald (1997)
γ	CRRA for upper-level utility function	1.5	N/A
$1 - \alpha^{NC}$	Non-college spending in A	41.5%	CEX
$1 - \alpha^C$	College spending in A	58.5%	
Z_A^{NC}	Non-college prod in A	0.33	QCEW
Z_A^C	College prod in A, normalized	1.14	
Z_B^{NC}	Non-college prod in B	0.47	
Z_B^C	College prod in B	0.66	
δ^A	Price adj. cost in A	190	Nakamura and Steinsson (2008)
δ^B	Price adj. cost in B	10	

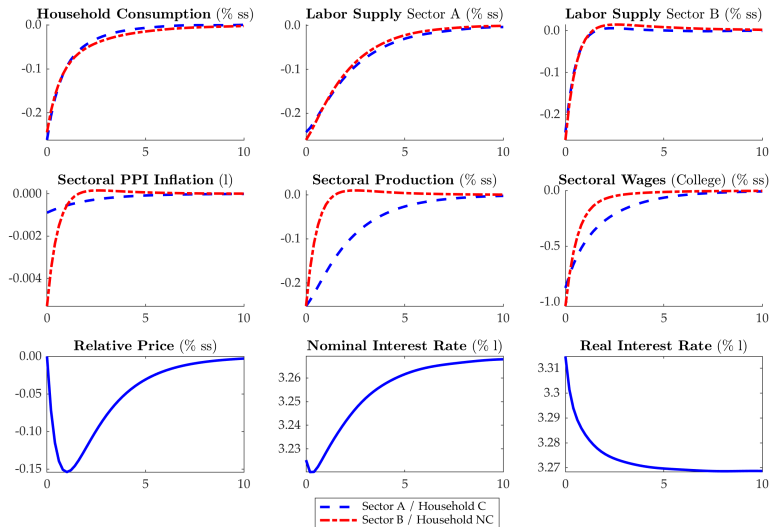
Baseline with 1 household type, 1 sector



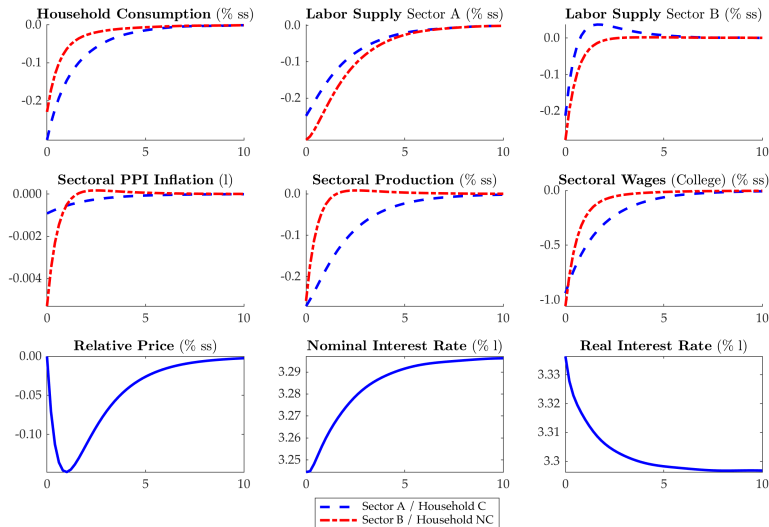
Introducing sectoral price rigidity heterogeneity



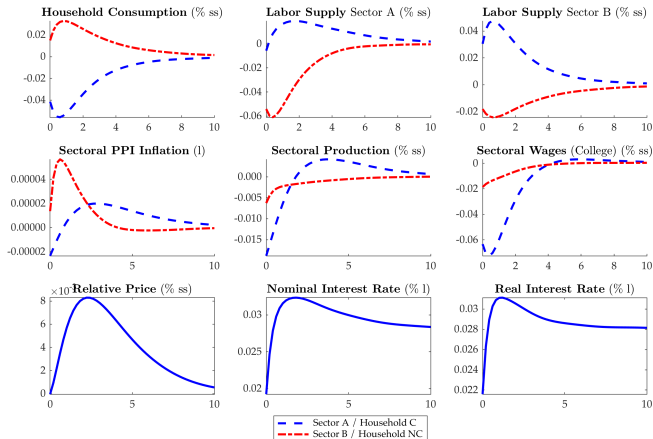
Comparison calibration: *add symmetric productivity differences*



Full calibration: *asymmetric productivity differences and tastes*

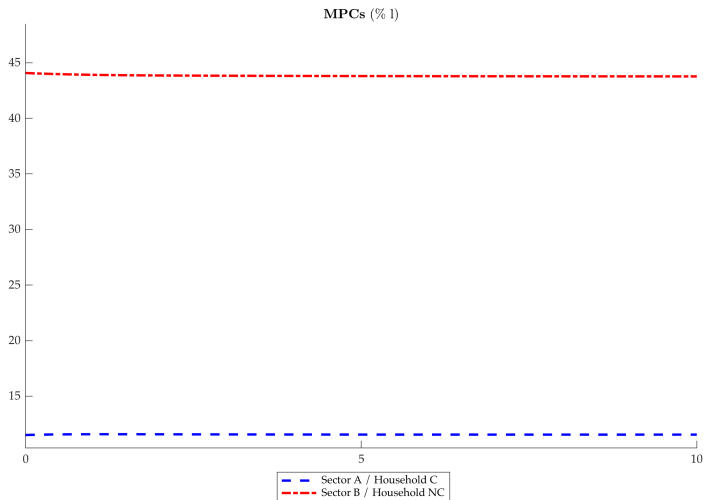


Differenced IRFs (Full – Comparison)



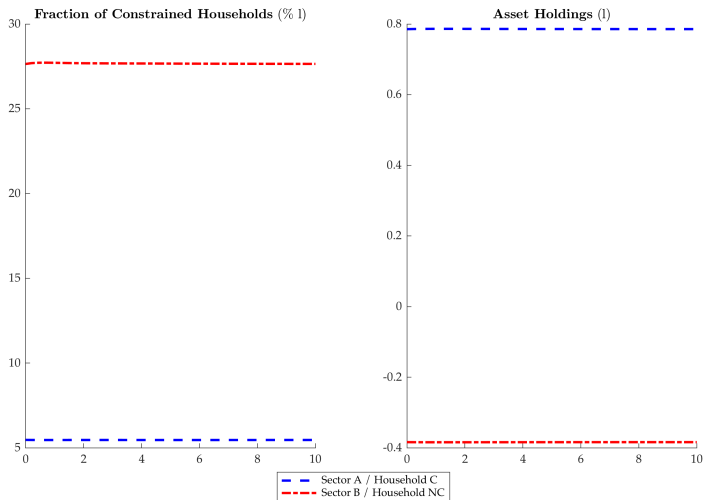
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Marginal propensities to consume (MPC)



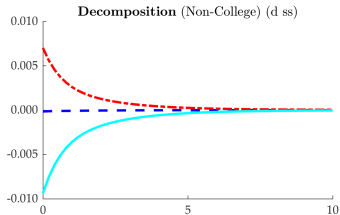
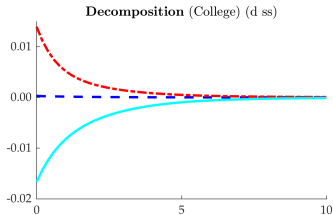
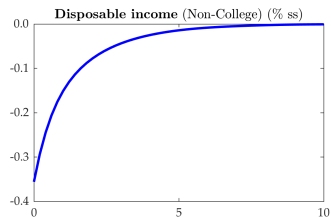
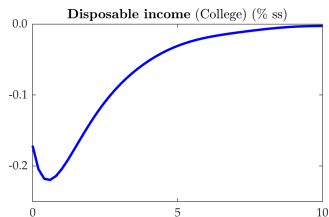
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Asset holdings and borrowing constraints



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Disposable income and its decomposition



— Asset income
- - - Transfer income
— Labor income

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Households' recursive optimization problem

- We collect households' state variables in the vector $x_{i,t}$ with law of motion

$$\begin{pmatrix} da_{i,t} \\ dz_{i,t} \end{pmatrix} = \begin{pmatrix} r_t a_{i,t} + \sum_s z_{i,t}^s n_{i,t}^s w_{i,t}^s p_t^{\alpha^i} - p_t^{\alpha^i} c_{i,t} + \frac{T_{i,t}}{P_t^A} \\ \mu(z_{i,t}^s) \end{pmatrix} dt + \begin{pmatrix} 0 \\ \sigma(z_{i,t}^s) \end{pmatrix} dB_t.$$

- This gives us the recursive, continuous-time Bellman equation

$$\begin{aligned} \rho v_{i,t}(x_{i,t}) = & \partial_t v_{i,t}(x_{i,t}) + \max_{c_{i,t}, n_{i,t}} u(c_{i,t}, n_{i,t}) + \theta_i \left(v_{-i,t}(x_{-i,t}) - v_{i,t}(x_{i,t}) \right) \\ & + \partial_a v_{i,t}(x_{i,t}) \left(r_t a_{i,t} + \sum_s z_{i,t}^s n_{i,t}^s w_{i,t}^s p_t^{\alpha^i} - p_t^{\alpha^i} c_{i,t} + \frac{T_{i,t}}{P_t^A} \right) \\ & + \mu(z_{i,t}^s) \partial_z v_{i,t}(x_{i,t}) + \frac{1}{2} \sigma(z_{i,t}^s)^2 \partial_{zz} v_{i,t}(x_{i,t}) \end{aligned}$$

- FOCs:

$$\begin{aligned} c_{i,t}^{-\gamma} &= p_t^{\alpha^i} \partial_a v_{i,t}(x_{i,t}) \\ c_{i,t}^{\gamma} (n_{i,t}^s)^{\phi} &= z_{i,t}^s w_{i,t}^s. \end{aligned}$$

The Taylor rule

- Assumptions on the Taylor rule are important
- For now, we assume equal weighting:

$$i_t = i_t^* + \sum_s \left(\phi_\pi^s \pi_t^s + \phi_y^s (Y_t^s - Y) \right) + \xi_t, \quad (1)$$

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Aggregation in our model

- We write Kolmogorov forward (KF) equations separately for each household type
- The KF equations characterizing the evolution of these density functions are given by

$$\begin{aligned}\partial_t g_{i,t}(x_{i,t}) = & -\partial_a \left(\left[r_t a_{i,t} + \sum_s z_{i,t}^s n_{i,t}^s w_{i,t}^s p_t^{\alpha^i} - p_t^{\alpha^i} c_{i,t} + \frac{T_{i,t}}{P_t^A} \right] g_{i,t}(x_{i,t}) \right) \\ & - \partial_z \left(\mu(z_{i,t}^s) g_{i,t}(x_{i,t}) \right) + \frac{1}{2} \partial_{zz} \left(\sigma(z_{i,t}^s)^2 g_{i,t}(x_{i,t}) \right) \\ & - \theta_i g_{i,t}(x_{i,t}) + \theta_{-i} g_{-i,t}(x_{-i,t}).\end{aligned}$$

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Channel decompositions

- Consider a perturbation $\{\xi_t\}$ that corresponds to a 100bps MP shock.
- We can decompose the effect on consumption as follows.

For College:

$$C_{C,0}(\{r_t, w_{C,t}, p_{C,t}, T_{C,t}\}_{t \in [0, \infty)}, g_0) \\ = \int_{\underline{a}}^{\infty} \int_{\underline{z}}^{\bar{z}} c_C(a, z, \{r_t, w_{C,t}, p_t, T_{C,t}\}_{t \in [0, \infty)}) g_0 d(z, a)$$

$$dC_{C,0} = \int_0^{\infty} \frac{\partial C_{C,0}}{\partial r_t} dr_t + \frac{\partial C_{C,0}}{\partial w_{C,t}} dw_{C,t} + \frac{\partial C_{C,0}}{\partial p_t} dp_t + \frac{\partial C_{C,0}}{\partial T_{C,t}} dT_{C,t} dt$$

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